

## Triaxial projected shell model study of $\gamma$ -vibrational bands in odd-neutron $^{105}\text{Mo}$ nucleus

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A unified description of nuclear excitations is one of the major research themes in nuclear structure physics. The possible modes of nuclear excitations are of single-particle, vibrational and rotational in character and in many nuclei these three modes coexist. One of the major challenges to nuclear models is to provide a unified description of these excitation modes. There is a long history of phenomenological models that were introduced to study the interplay among the three modes of excitations [1]. On the microscopic front, there are very few models capable of describing the three modes of excitations in a unified manner, in particular, at higher angular momenta. Mass  $\simeq 110$  region depicts some of the most interesting features in the nuclear periodic table. For instance, some nuclei in this region depict quite large deformation with  $\beta \simeq 0.45$  and is understood as due to the reinforcing effect of proton and neutron deformed shell gaps at  $Z=38, 40$  and  $N=60, 62$  [2]. Further, in some nuclei in this region, well developed  $\gamma$ - and  $\gamma\gamma$ - bands have been observed up to quite high angular momenta. For instance,  $\gamma$ - and  $\gamma\gamma$ - bands have been identified in  $^{104-106}\text{Mo}$  isotopes [3]. In neutron-rich odd-mass  $^{103-107}\text{Mo}$  collective band were investigated to higher spin including yrast bands as well as some side bands built on the single-neutron orbits. Although, yrast bands in this

region have been studied using theoretical approach of total routhian surface analysis, but there appears no systematic investigation of the  $\gamma$ -bands in this mass region [2].

Recently, the multi-quasiparticle TPSM approach has been employed to investigate the high-spin band structures in Er-isotopes and in the mass=130 region [4, 5]. It has been demonstrated in these studies that  $\gamma$ -bands are built on each intrinsic configuration of the mean-filed potential and generalizes the well known surface  $\gamma$ -vibration in deformed nuclei built on the ground-state configuration[3]. These recent developments in TPSM approach have greatly enhanced the model predictability and may provide new insights into the observed bands with unknown structures. As a matter of fact, by using this approach, the interpretation of complicated band structures has reached a quantitative level [6]. In the present work, we have further generalized the TPSM approach to study the  $\gamma$ -vibration in odd-mass nuclei. A preliminary application of this new development for the odd-proton system,  $^{103}\text{Nb}$ , has already been reported [7]. We have developed TPSM model to both odd-proton and odd-neutron systems and would like to investigate the observed  $\gamma$ -vibrational band structures in the mass  $\simeq 110$  region. In this mass region,  $\gamma$ -bands have been observed in even-even  $^{102-108}\text{Mo}$  and  $^{108-112}\text{Ru}$  nuclei, odd-neutron  $^{103-107}\text{Mo}$ , and odd-proton  $^{103}\text{Nb}$ . Further, this is the only region where  $\gamma$ - and  $\gamma\gamma$ -bands have been identified in odd-mass  $^{105}\text{Mo}$  and  $^{103}\text{Nb}$  nuclei [8].

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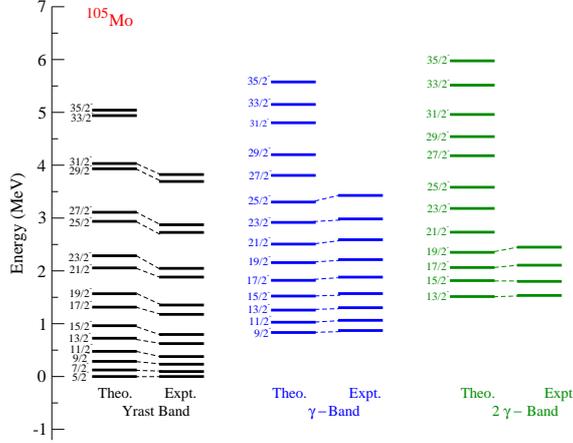


FIG. 1: The calculated yrast-,  $\gamma$ - and  $\gamma\gamma$ -bands of  $^{105}\text{Mo}$  are compared with the corresponding experimental data [9].

For the study of odd-neutron system, our model space is spanned by the following angular-momentum-projected one- and three-qp basis  $\{\hat{P}_{MK}^I a_n^\dagger \Phi, \hat{P}_{MK}^I a_n^\dagger a_{p1}^\dagger a_{p2}^\dagger \Phi\}$ . The qp basis chosen is adequate to describe high-spin states up to  $I \sim 20\hbar$  for even-even system,  $I \sim 35/2\hbar$  for even-odd and odd-even nuclei considered in this work. In the present analysis we shall, therefore, restrict our discussion to this spin regime. For the self-conjugate vacuum or 0-qp state,  $\kappa = 0$  and, therefore, it follows from the above equation that only  $K =$  even values are permitted for this state. For 2-qp states,  $a^\dagger a^\dagger |\Phi\rangle$ , the possible values for  $K$ -quantum number are both even and odd, depending on the structure of the qp state. For example, for a 2-qp state formed from the combination of the normal and the time-reversed states  $\kappa = 0$ , only  $K =$  even values are permitted. For the combination of the two normal states,  $\kappa = 1$  and only  $K =$  odd states are permitted. For one-qp state,  $\kappa = 1/2$  ( $-1/2$ ), and the possible values of  $K$  are therefore  $1/2, 5/2, 9/2, \dots$  ( $3/2, 7/2, 11/2, \dots$ ).

In the present calculation the triaxial Nilsson mean-field Hamiltonian, which can be obtained by using the Hartree-Fock-Bogoliubov (HFB) approximation, employed is given by

$$\hat{H}_N = \hat{H}_0 - \frac{2}{3}\hbar\omega \left\{ \epsilon \hat{Q}_0 + \epsilon' \frac{\hat{Q}_{+2} + \hat{Q}_{-2}}{\sqrt{2}} \right\}. \quad (1)$$

The interaction strengths are taken as follows: The QQ-force strength  $\chi$  is adjusted such that the physical quadrupole deformation  $\epsilon$  is obtained as a result of the self-consistent mean-field HFB calculation. The monopole pairing strength  $G_M$  is of the standard form  $G_M = (20.12 \mp 13.13 \frac{N-Z}{A}) \frac{1}{A}$  (MeV), where  $-(+)$  is neutron (proton). The configuration space used is ( $\pi = 3, 4, 5$  for protons and  $\nu = 4, 5, 6$  for neutrons). The TPSM study has been performed for odd-neutron  $^{105}\text{Mo}$  nucleus. The axial and non-axial deformations used in the present work are 0.300 and 0.110 respectively. Non-axial deformations have been ascertained from the PES calculations, wherever a minimum was obtained, otherwise fitted to reproduce the  $\gamma$ -band head energy.

The TPSM results for  $^{105}\text{Mo}$ , Fig. 1, show a very nice agreement with the agreement with the experimental data for the yrast and as well for  $\gamma$ - and  $\gamma\gamma$ -bands. This is the only odd-neutron system in which both  $\gamma$ - and  $\gamma\gamma$ -bands have been observed upto high spin [9].

## References

- [1] A. Bohr and B. R. Mottelson, *Nuclear Structure*, Vol. II (Benjamin Inc., New York, 1975).
- [2] J. H. Hamilton et al., Prog. Part. Nucl. Phys. **35**, 635 (1995).
- [3] A. Guessous et al., Phys. Rev. Lett. **75**, 2280 (1995).
- [4] J. A. Sheikh, G. H. Bhat, et al., Phys. Rev. **C 77**, 034313 (2008).
- [5] J. A. Sheikh, G.H. Bhat, et al., Nucl. Phys. **A 824**, 58 (2009).
- [6] E. Y. Yeoh et al., Phys. Rev. **C 83**, 054317 (2011).
- [7] J. A. Sheikh, G.H. Bhat, Y. Sun, and R. Palit, Phys. Lett. **B 688**, 305 (2010).
- [8] M. A. C. Hotchkis et al., Nucl. Phys. **A 530**, 111 (1991).
- [9] H. B. Ding, et al., Phys. Rev. **C 74**, 054301 (2006).