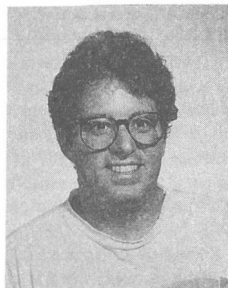


## Measurement of $\sigma * BR(W + \gamma)$ and $\sigma * BR(Z + \gamma)$ at CDF

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### Abstract

We have measured the cross section  $\times$  branching ratio for  $W + \gamma$  and  $Z + \gamma$  in the electron and muon channels using the  $W$  and  $Z$  data samples from the CDF '88-'89 collider run, in  $4.05 \pm 0.28 \text{ pb}^{-1}$  ( $3.54 \pm 0.24 \text{ pb}^{-1}$ ) of electron (muon) data. For central photons with  $E_T^{\gamma} > 5.0 \text{ GeV}$  and  $\Delta R_{l\gamma} > 0.7$ , we observe 8 (5) electron (muon)  $W\gamma$  candidates and 2 (2) electron (muon)  $Z\gamma$  candidates. From these events, we measure  $\sigma * BR(W\gamma) = 17.9^{+11.1}_{-10.7} \text{ (stat + syst) pb}$  and  $\sigma * BR(Z\gamma) = 9.2^{+5.2}_{-5.1} \text{ (stat + syst) pb}$  for the  $e + \mu$  combined sample. From the  $W\gamma$  cross section  $\times$  branching ratio measurement, we obtain limits on anomalous  $WW\gamma$  couplings of the  $-6.5 < \Delta\kappa < +6.9$  ( $\lambda = 0$ ) and  $-3.1 < \lambda < +3.1$  ( $\Delta\kappa = 0$ ) at the 95% CL.

## 1 Introduction

The Standard Model (SM) unifies the electromagnetic and weak interactions into a single interaction described by the gauge group  $SU(2)_L \otimes U(1)_Y$ . This theory predicts the existence of the  $W^\pm$  vector bosons as carriers of the charged weak currents and two neutral vector bosons as carriers of the neutral currents, the  $\gamma$  and the  $Z^0$ . The measurement of  $W$  and  $Z$  production cross sections and decay properties at  $\sqrt{s} = 1.8 \text{ TeV}$   $\bar{p}$ - $p$  collisions tests the strength and the nature of the couplings of gauge boson to quarks and leptons. The measurement of the  $W^\pm\gamma$  and  $Z^0\gamma$  production cross sections and final-state kinematics provides an experimental test of the trilinear gauge boson couplings and also simultaneously yields new information on static electromagnetic multipole moments of the  $W$  boson[2,3].

## 2 Data Samples

The  $W\gamma$  and  $Z\gamma$  candidate events were obtained from the 1988-89 inclusive  $W$  and  $Z$  data sets, which were used for the electron and muon  $W$  and  $Z$  cross-section  $\times$  branching ratio measurements and the electron and muon  $W/Z$  cross-section ratios [4]. A total of  $\int \mathcal{L}_e dt = 4.05 \pm 0.28 \text{ pb}^{-1}$  of electron data and  $\int \mathcal{L}_\mu dt = 3.54 \pm 0.24 \text{ pb}^{-1}$  of muon data were collected this run[4].

Each of the inclusive  $W$  and  $Z$  data sets require at least one well measured, isolated, high transverse momentum ( $P_T$ ) lepton in a good fiducial region of the central electromagnetic calorimeter ( $CEM$ ) for electrons and central muon chambers ( $CMU$ ) for muons. Additionally,  $W$  events must contain a neutrino whose signature is large missing transverse energy ( $E_T > 20 \text{ GeV}$ ).  $Z^0$  events require a second lepton and have a dilepton mass in a window centered on the  $Z^0$  mass. The  $Z$  events are removed from the  $W$  data sample. The precise description of the  $W$  and  $Z$  selection in the electron and muon channels can be found in [4].

The electron and muon  $W\gamma$  and  $Z\gamma$  sub-datasets are formed by requiring an additional isolated well-measured photon passing the following criteria: the EM cluster have  $|\eta_\gamma| < 1.1$ ; be within a good fiducial region of CEM calorimeter; the extra transverse energy deposited in a cone  $\Delta R = 0.4$  centered on the photon, but not including the photon:  $E_T^{\text{cone}} - E_T^{\text{photon}} < 2.0 \text{ GeV}$  (*Calorimeter isolation*); the sum of the transverse momentum due to charged tracks within a cone of  $\Delta R = 0.4$  centered on the photon:  $\sum P_T^{\text{cone}}(\Delta R = 0.4) < 2.0 \text{ GeV}$  (*tracking isolation*); no three dimensional tracks pointing at the EM cluster; electromagnetic energy fraction of the EM cluster be consistent with photons; transverse shower shape in the  $CEM$  calorimeter towers be consistent with testbeam photons; transverse shower shape in the proportional chamber at EM shower maximum ( $CES$ ) be consistent with photons in both views  $r - \phi$  and  $z(\eta)$ ; no other clusters of energy in the  $CES$  detector (within the  $CEM$  cluster) in either the  $z$  or  $r - \phi$  views with  $E > 1.0 \text{ GeV}$ ; and an angular separation between the  $W/Z$  decay lepton(s) and the photon  $\Delta R_{l\gamma} > 0.7$ . The isolation cuts are designed to reduce the QCD background. Requiring no second  $CES$  cluster further suppresses the  $\pi^0$  and other multi-photon backgrounds. The  $\Delta R_{l\gamma}$  cut is designed to suppress the contribution of radiative decay (as opposed to  $W/Z \gamma$  production) in the signal. The overall efficiency for finding  $CEM$  photons was determined to be  $\epsilon_\gamma = 80 \pm 1\%$ . We observe 8(5) electron (muon)  $W\gamma$  and 2(2) electron (muon)  $Z\gamma$  candidates.

## 3 Backgrounds

The largest photon background in the  $W\gamma$  and  $Z\gamma$  signal is due to the combination of a QCD jet faking a photon and to a lesser extent prompt isolated photons due to initial/final state radiation (quark QED bremsstrahlung). The photon backgrounds due to QCD jets in the inclusive electron and muon  $W$  and  $Z$  data samples were determined using a multi-jet data sample. This QCD sample required two high  $E_T$  jets (*leading*) kinematically similar to jets from hadronic  $W(Z)$  decay. The other (*non-leading*) jets in the event were used to measure the fragmentation rate. The non-leading jets were required to pass all photon selection cuts. The probability of jet to pass all  $\gamma$  cuts is  $\approx 0.2\%$ .

As a cross-check on the determination of QCD backgrounds for each of the four  $W/Z$  data samples, VECBOS [5] + Herwig MC + CDF detector simulation was used to generate  $W/Z + n$  jets ( $n_{jets} \leq 2$  jets). These events were then required to pass all  $W\gamma/Z\gamma$  cuts. The systematic uncertainty on the QCD background for each of the four channels is defined as the difference between the QCD background derived from the QCD data sample and the the QCD background derived from the  $W/Z + jets$  Monte Carlo simulation. Other backgrounds to  $W\gamma$  and  $Z\gamma$  physics include  $Z + \gamma$  and  $Z + jet - faking\ photon$  where one of the leptons from  $Z^0$  decay is not detected and the  $Z$  is misidentified as a  $W$ . The proceses  $(W \rightarrow \tau\nu_\tau) + \gamma$  and  $(W \rightarrow \tau\nu_\tau) + Jet$  can also contribute to the background in the electron and muon  $W\gamma$  data samples when the  $\tau$  decays to an electron or muon, respectively. The corresponding processes  $(Z \rightarrow \tau^+\tau^-) + \gamma$  and  $(Z \rightarrow \tau^+\tau^-) + Jet$  contribute negligibly to the background in the electron and muon  $Z\gamma$  data samples. The Drell-Yan contributions to  $Z\gamma$  in the  $M_{\ell^+\ell^-}$  mass window used is also small ( $< 3\%$ ). Table 1 contains a summary of the backgrounds for  $W\gamma/Z\gamma$ .

Table 1 - Backgrounds for  $W\gamma$  and  $Z\gamma$ 

Channel	$N_{QCD}^V$	$N^{Z\gamma} + N_{QCD}^{Z\gamma}$	$N^{Wre}$
$W(e\nu)\gamma$	$3.57 \pm 0.81 \pm 1.47$	$0.14 \pm 0.02 \pm 0.07$	$0.11 \pm 0.01$
$W(\mu\nu)\gamma$	$1.87 \pm 0.42 \pm 0.84$	$0.44 \pm 0.07 \pm 0.12$	$0.06 \pm 0.01$
$Z(e^+e^-)\gamma$	$0.30 \pm 0.07 \pm 0.14$	—	—
$Z(\mu^+\mu^-)\gamma$	$0.11 \pm 0.03 \pm 0.04$	—	—

#### 4 Determination of $\sigma * BR(W + \gamma)$ and $\sigma * BR(Z + \gamma)$

The  $W\gamma$  and  $Z\gamma$  Monte Carlo programs developed by Ulrich Baur[6] were used to generate electron, muon and tau  $W\gamma$  and  $Z\gamma$  data samples. This data coupled with a "fast" and very detailed MC detector simulation was used to determine geometric and kinematic acceptances. In addition,  $W\gamma$  and  $Z\gamma$  cross sections were obtained for events passing the  $W$  and  $Z$  boson event selection, the  $\Delta R_{\ell-\gamma} > 0.7$  and  $E_T^\gamma > 5.0$  GeV photon cuts. This MC data was used to make predictions on the expected number of  $W\gamma$  and  $Z\gamma$  events in the CDF electron and muon  $W\gamma$  and  $Z\gamma$  data samples, entering all relevant electron, muon and photon *efficiencies*.

The experimental results for the cross-section  $\times$  branching ratio in the electron/muon channels were determined from

$$\sigma_V \cdot B(V + \gamma) = \frac{\mathcal{N}_{observed}^{V\gamma} - \sum \mathcal{N}_{background}^{V\gamma}}{A_{V\gamma} \cdot \epsilon_{V\gamma} \cdot \int \mathcal{L}_t dt} = \frac{\mathcal{N}_{signal}^{V\gamma}}{A_{V\gamma} \cdot \epsilon_{V\gamma} \cdot \int \mathcal{L}_t dt} \quad (1)$$

where  $V = W$  or  $Z$ ,  $A_{V\gamma} \cdot \epsilon_{V\gamma}$  is the product of the acceptances  $\times$  efficiency factors for detecting  $V\gamma$  events and  $\ell = e$  or  $\mu$ .

We can derive the *combined* electron and muon  $\sigma \cdot BR(W + \gamma)$  and  $\sigma \cdot BR(Z + \gamma)$  using a method similar to that used for determining the  $\sigma \cdot BR(V + \gamma)$  for the individual channels. If we assume lepton universality, the combined  $\sigma \cdot BR(V + \gamma)$  can be written as:

$$\sigma * BR(V + \gamma) = \frac{N_e^{signal} + N_\mu^{signal}}{\int \mathcal{L}_e dt \cdot A_e^{V\gamma} \cdot \epsilon_e^{V\gamma} + \int \mathcal{L}_\mu dt \cdot A_\mu^{V\gamma} \cdot \epsilon_\mu^{V\gamma}} \quad (2)$$

We see in table 2 that the cross section  $\times$  branching ratio for both channels and the combined results of  $W\gamma$  and  $Z\gamma$  are good agreement with the SM predictions.

Table 2 -  $\sigma * BR$  for  $W\gamma$  and  $Z\gamma$ 

Process	$e$ (pb)	$\mu$	$e + \mu$	SM
$\sigma * BR(W\gamma)$	$17.0^{+13.7}_{-13.4} (stat + syst)$	$19.4^{+18.3}_{-17.9}$	$17.9^{+11.1}_{-10.7}$	$19.0^{+3.3}_{-0.9}$
$\sigma * BR(Z\gamma)$	$6.8^{+5.7}_{-5.7} (stat + syst)$	$13.6^{+10.3}_{-10.1}$	$9.2^{+5.2}_{-5.1}$	$4.7^{+0.7}_{+0.2}$

## 5 Limits on Anomalous Couplings for $W\gamma$

The Baur  $W\gamma$  MC coupled with a fast detector simulation was used to obtain 68.3%, 90% and 95% CL upper limits for  $\Delta\kappa = \kappa - 1$  and  $\lambda$  parameters on a grid of 80  $\Delta\kappa$  and  $\lambda$  points. The MC  $\sigma \cdot BR(W\gamma)$  data is then fit using MINUIT to obtain a 3-dimensional description of the  $\sigma \cdot BR(W\gamma)$  cross section surface in the  $\Delta\kappa - \lambda$  plane. The parametrization of the fit is of the following form:

$$\sigma(\Delta\kappa, \lambda) = \sigma_{SM} + a\Delta\kappa + b\Delta\kappa^2 + c\lambda + d\lambda^2 + e\Delta\kappa\lambda \quad (3)$$

No higher-order terms in  $\Delta\kappa, \lambda$  are needed, since the invariant amplitude  $\mathcal{M}$  containing the anomalous contributions to the  $W\gamma$  process is *linear* in the anomalous parameters  $\kappa$  and  $\lambda$ ; the term  $e\Delta\kappa\lambda$  is due to the interference between the various amplitudes associated with the  $W\gamma$  process. Figure 1 shows the projection of the  $W\gamma$  cross section on the  $\kappa$  or  $\lambda$  axis. The central value of the combined  $e + \mu \sigma \cdot BR(W + \gamma)$  experimental result is shown as a horizontal solid line, the  $\pm 1\sigma$  (stat+syst) (68% double-side CL) are shown as horizontal dashed lines; the 90% and 95% single sided CL are also shown. Figure 2 contains the 68.3%, 90% and 95% single sided CL contours in the  $\Delta\kappa - \lambda$  for the combined  $e + \mu W\gamma$  results. Note, the displacement of the location of the minimum of the  $\sigma \cdot BR(W + \gamma)$  cross section relative to the SM value.

The UA2 experiment recently published limits on  $\kappa$  and  $\lambda$  from an analysis of 13  $pb^{-1}$  of electron  $W\gamma$  data using two different methods: the first method is equivalent to ours, comparing the number of signal events to the number of predicted events, and the second method obtained limits by fitting the  $P_T^\gamma$  spectrum[7]. Our results are comparable with the UA2 results; the results from both experiments are summarized in Table 3.

Table 3: CDF vs UA2 Comparison of  $\Delta\kappa - \lambda$  Limits

Parameter	CL Range	CDF $e + \mu$ Limits	UA2 $\sigma \cdot B$	UA2 $P_T^\gamma$ Method
$\Delta\kappa$ ( $\lambda = 0$ )	68.3% DS	$0.0_{-4.2}^{+4.7}(stat) \pm 0.6(syst)$	$0.0_{-4.2}^{+4.6}(stat) \pm 1.0(syst)$	$0.0_{-2.2}^{+2.6}(stat)$
	68.3% SS	$-3.2 < \Delta\kappa < +3.7$	—	—
	90.0% SS	$-5.7 < \Delta\kappa < +6.1$	—	—
	95.0% SS	$-6.5 < \Delta\kappa < +7.0$	$-6.3 < \Delta\kappa < +6.9$	$-4.5 < \Delta\kappa < +4.9$
$\lambda$ ( $\Delta\kappa = 0$ )	68.3% DS	$0.0_{-2.0}^{+2.0}(stat) \pm 0.3(syst)$	$0.0_{-2.9}^{+2.9}(stat) \pm 0.7(syst)$	$0.0_{-1.8}^{+1.7}(stat)$
	68.3% SS	$-1.6 < \lambda < +1.6$	—	—
	90.0% SS	$-2.7 < \lambda < +2.7$	—	—
	95.0% SS	$-3.1 < \lambda < +3.1$	$-4.4 < \lambda < +4.4$	$-3.6 < \lambda < +3.5$

Since the  $W$  boson magnetic dipole moment  $\mu_W = \frac{e}{2M_W}(2 + \Delta\kappa + \lambda)$ , electric quadrupole moment  $Q_W = -\frac{e}{M_W^2}(1 + \Delta\kappa - \lambda)$  and the  $W$  boson mean-squared charge radius  $\langle R_W^2 \rangle = \frac{1}{M_W^2}(1 + \Delta\kappa + \lambda)$  are related to  $\Delta\kappa$  and  $\lambda$ , we can derive the limits on the  $EM$  moments. In the SM (at tree level):  $\Delta\kappa = 1 - \kappa = 0$ ,  $\lambda = 0$ ; in the SM  $\mu_W^0 = \frac{e\hbar c}{2M_W c^2}$  and  $Q_W^0 = -e\left(\frac{\hbar c}{M_W c^2}\right)^2 = -e\lambda_W^2$  where  $\lambda_W$  is the (reduced) Compton wavelength for the  $W$  boson. Table 4 summarizes the combined  $e + \mu$  limits on the  $W$  electromagnetic moments  $\mu_W$  and  $Q_W$ . Figure 3 shows the 68.3%, 90.0% and 95.0% single-sided CL contours in the  $Q_W/Q_W^0 - \mu_W/\mu_W^0$  plane for the combined  $e + \mu$  results.

Table 4: CDF Limits on  $W$  Boson  $EM$  Moments

Parameter	CL Range	CDF $e + \mu$ Limits
$\mu_W/\mu_W^0$	68.3% <i>DS CL</i>	$2.0^{+3.2}_{-3.1} (stat) \pm 0.5 (syst) = 2.0^{+3.6}_{-3.6} (stat + syst)$
$(Q_W/Q_W^0 = 1)$	68.3% <i>SS CL</i>	$-2.4 < \mu_W/\mu_W^0 - 2 \equiv g_W - 2 < +2.5$
	90.0% <i>SS CL</i>	$-4.2 < \mu_W/\mu_W^0 - 2 \equiv g_W - 2 < +4.2$
	95.0% <i>SS CL</i>	$-4.8 < \mu_W/\mu_W^0 - 2 \equiv g_W - 2 < +4.9$
$Q_W/Q_W^0$	68.3% <i>DS CL</i>	$1.0^{+4.9}_{-4.5} (stat) \pm 0.7 (syst) = 1.0^{+5.6}_{-5.2} (stat + syst)$
$(\mu_W/\mu_W^0 = 2)$	68.3% <i>SS CL</i>	$-3.5 < Q_W/Q_W^0 - 1 \equiv q_W - 1 < +3.8$
	90.0% <i>SS CL</i>	$-6.1 < Q_W/Q_W^0 - 1 \equiv q_W - 1 < +6.4$
	95.0% <i>SS CL</i>	$-7.0 < Q_W/Q_W^0 - 1 \equiv q_W - 1 < +7.4$
$< R_W >^2 / \lambda_W^2$	68.3% <i>DS CL</i>	$1.0^{+3.2}_{-3.1} (stat) \pm 0.5 (syst) = 1.0^{+3.6}_{-3.6} (stat + syst)$
$(Q_W/Q_W^0 = 1)$	68.3% <i>SS CL</i>	$-2.4 < < R_W >^2 / \lambda_W^2 - 1 \equiv r_W^2 - 1 < +2.5$
	90.0% <i>SS CL</i>	$-4.2 < < R_W >^2 / \lambda_W^2 - 1 \equiv r_W^2 - 1 < +4.2$
	95.0% <i>SS CL</i>	$-4.8 < < R_W >^2 / \lambda_W^2 - 1 \equiv r_W^2 - 1 < +4.9$

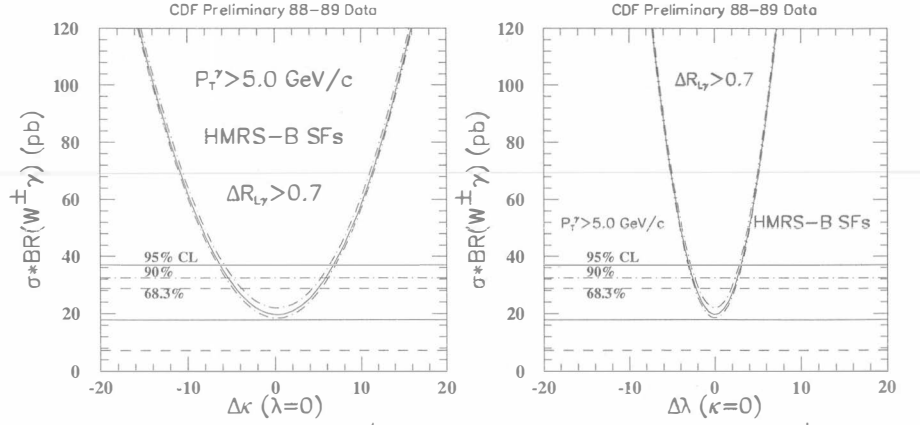
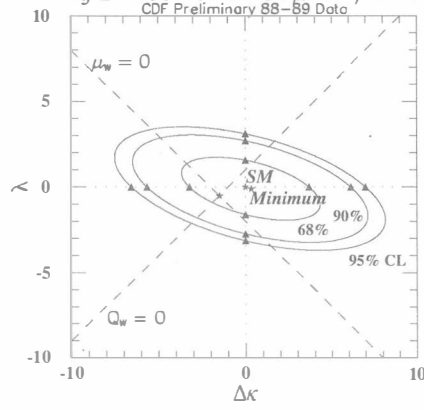
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Fig 1 - Combined  $e+\mu$   $\sigma \cdot BR(W^\pm \gamma)$ Fig 2 - Combined  $e+\mu$   $W^\pm \gamma$   $\lambda - \Delta\kappa$ Fig 3 - Combined  $e+\mu$   $W^\pm \gamma$   $Q_W - \mu_W$ 