Review of Nucleon Decay Searches at Super-Kamiokande

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Baryon number violation appears in many contexts. It is a requirement for baryogenesis and is a consequence of Grand Unified Theories (GUTs), which predict nucleon decay. Nucleon decay searches provide the most direct way to test baryon number conservation and also serve as a unique probe of GUT scale physics around 10^{14-16} GeV. Such energies cannot be reached directly by accelerators. However, they can be explored indirectly at large underground water Cherenkov (WC) experiments, which due to the size of their fiducial volume are highly sensitive to nucleon decays. We review searches for baryon number violating processes at the state of the art WC detector, the Super-Kamiokande. Analyses of the typically dominant non-SUSY and SUSY nucleon decay channels such as $p \to (e^+, \mu^+)\pi^0$ and $p \to \nu K^+$, as well as more exotic searches, will be discussed. Presented studies set the world's best limits, which circumvent the allowed parameter space of theoretical models.

1 Motivation

Baryon number (B) is a global accidental symmetry of the Standard Model (SM) and ensures that the lightest baryon (proton) is stable. However, not only is it violated by non-perturbative effects within the SM itself [1], baryon number violation (\cancel{B}) is a required condition for explaining the observed matter - anti-matter asymmetry of the universe [2]. More so, various theoretical arguments as well as reductionism hint at the SM being an incomplete theory and that there exists a more unifying underlying account. Such an account could be provided by Grand Unified Theories (GUTs) [3, 4, 5], like SU(5) and SO(10), which unite the three SM gauge groups together $G_{GUT} \supset SU(3)_C \otimes SU(2)_W \otimes U(1)_Y$ and offer an explanation for charge quantization as well as coupling unification. With quarks and leptons appearing within a common GUT representation, one can transform into another, giving rise to nucleon decay (explicit \cancel{B}). In the more fundamental domain of quantum gravity, it is expected [6] that global symmetries, such as B, are violated in general. The presence of nucleon decay could also have profound consequences for the future fate of the universe [7]. For a topical review of B-violation as well as nucleon decay predictions see Ref. [8] and Ref. [9], respectively.

While there is no convincing evidence of *B*-violation thus far, testing *B* remains a high priority. Nucleon decay can provide not only one of the most striking signatures of *B*-violation, but it also offers a unique way of testing Grand Unified Theories. With the unification scale being around $10^{15\pm1}$ GeV, Grand Unified Theories cannot be probed directly by accelerators. However, they can be examined indirectly with large underground water Cherenkov experiments, which due to the size of their fiducial volume are highly sensitive to nucleon decays. Below, we review the nucleon decay search results from the current state of the art WC experiment, the Super-Kamiokande (SK, Super-K).

2 The Super-Kamiokande Experiment

Super-Kamiokande is a 50 kiloton WC detector (22.5 kiloton fiducial volume) located beneath a one-km rock overburden (2700 m. water equivalent) within the Kamioka mine in Japan. The SK detector is composed of an inner (11,146 inward-facing 20-inch PMTs, providing 40% photo-coverage) and an outer (1,855 8-inch outward-facing PMTs) detector, which are optically separated. Cherenkov radiation [10], produced by charged particles traveling through water, is collected by the PMTs and is used to reconstruct the physics events.

Data collected by Super-Kamiokande (SK) during the periods of SK-I (May 1996-Jul. 2001, 1489.2 live days), SK-II a (Jan. 2003- Oct. 2005, 798.6 live days), SK-III (Sep. 2006-Aug. 2008, 518.1 live days) and the ongoing SK-IV b experiment (Sep. 2008-present, > 1500 live days) corresponds to a combined exposure of more than 250 kiloton-yrs. Details of the detector design, performance, calibration, data reduction and simulation can be found in Ref. [11, 12].

The experiment allows one to study a wide variety of physics topics in the MeV - TeV energy range, including those related to solar and atmospheric neutrinos (oscillations, tests of Lorentz invariance, day-night asymmetry, sterile neutrino, indirect dark matter searches), supernovae relic neutrinos as well as nucleon decay.

3 Nucleon Decay Searches

For nucleon decay analyses, only events for which all of the observed Cherenkov light was fully contained within the inner detector are considered. The observed Cherenkov rings are classified either as showering ("e-like", for e^{\pm} and γ) or non-showering (" μ -like", for μ^{\pm}). We do not distinguish between signal channels with a ν and $\overline{\nu}$ in the final state, since neither of the neutrinos is observable.

In the signal Monte Carlo (MC) simulations, the effects of Fermi momentum, nuclear binding energy as well as nucleon-nucleon correlated decays are taken into account [13]. The atmospheric neutrino background interactions are generated using the neutrino flux calculations of Honda *et. al.* [14] and the NEUT simulation package [15], which uses a relativistic Fermi gas model. The SK detector simulation software is based on the GEANT-3 [16] package. Background MC corresponding to a 500 year detector exposure-equivalent is generated for each SK period.

3.1 $p \rightarrow e^+ \pi^0$ and $p \rightarrow \mu^+ \pi^0$

The $p \to e^+\pi^0$ channel is often the most dominant nucleon decay mode in GUTs, with typical lifetime predictions of 10^{29-36} yrs. Previous searches for this channel have already excluded minimal SU(5) [17, 18, 19, 20]. Within some models (e.g. flipped SU(5) [21]), a similar channel, $p \to \mu^+\pi^0$, can also appear with a significant branching ratio.

Since e^+ , $\mu^+(\to e^+\nu\nu)$ as well as $\pi^0(\to\gamma\gamma)$ produce visible Cherenkov rings, one can fully reconstruct the invariant mass and momentum of the parent proton. Figure 1 displays the signal MC, background MC and data (306 kiloton yrs of exposure), after all the event selection criteria have been applied. The signal region consists of two portions, a "lower box" (free protons) and an "upper box" (bound protons), separated in the analysis for improved sensitivity. For $p \to e^+\pi^0$, the average signal efficiency as well as the total expected background within the selected region is 38.7% and 0.61 events, respectively. For $p \to \mu^+\pi^0$, it is 34.6% and 0.87 events, respectively. No data events pass the selection for $p \to e^+\pi^0$, while two events pass for $p \to \mu^+\pi^0$. The Poisson probability of observing two such events for a given exposure is 23%. Since both events also display background-like features, they are judged as coming from atmospheric- ν background. Hence, the 90% confidence level (C.L.) lower lifetime limits of 1.7×10^{34} yrs. and 7.8×10^{33} yrs. are placed on the $p \to e^+\pi^0$ and $p \to \mu^+\pi^0$ channels [22], respectively.

 $[^]a{\rm An}$ accident caused SK-II photo-coverage to be reduced to 20%. Full photo-coverage was restored in SK-III. $^b{\rm Electronics}$ have been upgraded in SK-IV.



Figure 1 – Reconstructed invariant mass vs. total momentum for $p \to e^+ \pi^0$ [left] and $p \to \mu^+ \pi^0$ [right]. The left panels show signal MC, where light blue corresponds to free protons and dark blue to bound protons. The middle panels show atmospheric- ν MC and the right panels show data. From Ref. [22].

The analyses for the other $p \to l^+ + m^0$ and $n \to l^- + m^+$ searches are conducted in a similar manner. Here, $l^{\pm}(e^{\pm}, \mu^{\pm})$ represents a charged lepton, while $m^0(\omega^0, \eta, \rho^0, K^0)$ and $m^+(\pi^-, \rho^-)$ denote a neutral and a charged meson, respectively. No significant signal excess is observed in any of these channels, resulting in the 90 % C.L. lower lifetime limits of around 10^{32-33} years [13, 23].

3.2 $p \rightarrow \nu K^+$

The introduction of supersymmetry (SUSY), which is theoretically well motivated, allows one to make GUT coupling unification precise. New operators come into play and typically the dominant SUSY GUT mode is $p \to \nu K^+$, with lifetime predictions around 10^{29-36} yrs. Previous searches for this channel have already excluded minimal (TeV-)SUSY SU(5) [24]. Since neutrino



Figure 2 – Results for three different $p \rightarrow \nu K^+$ search methods. promt- γ tagging [left], μ^+ momentum [center] and visible energy for π^+ [right]. The signal MC, atmospheric ν MC and data are shown in blue, red, and black, respectively. From Ref. [25].

and the kaon are invisible (kaon below Cherenkov threshold) in this mode, reconstruction of the parent nucleon is not possible. However, analysis can be done on the kaon decay products, coming from the $K \to \mu^+ \nu$ (Br. 64%) and $K \to \pi^+ \pi^0$ (Br. 21%) channels. Three different analyses are performed at SK. The first search is done in the muon channel, where a prompt- γ , which could appear from nuclear de-excitation after the proton has decayed, is tagged. The second search is also done in the muon channel, where a spectral χ^2 fit to the μ^+ momentum is performed. The third search is done in the pion channel, where the $\pi^0(\to \gamma\gamma)$ is reconstructed and the visible energy from π^+ is analyzed. Figure 2 displays the signal MC, background MC and data (260 kiloton-yrs exposure), after all the event selection criteria have been applied. The average efficiency and background for the three searches is 7.9% and 0.39 events, 33.7% and 579.4 events and 8.2% and 0.56 events for the prompt- γ , μ -spectrum and the pion search.

respectively. No significant excess is observed and a 90% C.L. lower lifetime limit of 6.6×10^{33} yrs. is placed on this channel [25].

3.3 $n-\overline{n}$

For this mode, $\Delta B = 2$ and it parametrizes the scale of $U(1)_{B-L}$ symmetry breaking. The process is naturally connected with baryogenesis as well as neutrinos, since Majorana neutrinos and the see-saw mechanism require $\Delta L = 2$. Since the effective operator corresponding to this process has dimension nine, $n - \overline{n}$ can be viewed as a probe of intermediate $10^3 - 10^{11}$ GeV scale physics [26]. When the resulting \overline{n} is captured by a p or n, a variety of mesons (predominantly



Figure 3 – Reconstructed invariant mass vs. total momentum for $n - \overline{n}$. The signal MC, atmospheric ν MC and data are displayed on the left (red), center (blue) and right (black) panels, respectively. From Ref. [27].

pions) are released. This can be used to reconstruct the invariant mass and momentum of the original "di-nucleon" $\overline{n}p$ or $\overline{n}n$ systems and perform a search analysis similar to $p \to e^+\pi^0$. Figure 3 displays the signal MC, background MC and data (91.5 kiloton-yrs exposure), after all the event selection criteria have been applied. The efficiency and expected background for this search is 12.1% and 24 events, respectively. No significant excess is observed and a 90% C.L. lower lifetime limit of 1.9×10^{32} yrs.^c is obtained [27].

3.4 $np, nn, pp \rightarrow mesons$

Similar to $n - \overline{n}$, di-nucleon decays of np, nn and pp are $\Delta B = 2$ processes and can provide novel insights beyond the single nucleon decay searches. The di-nucleon decay channels $np \to \pi^+\pi^0, nn \to \pi^0\pi^0$ and $pp \to \pi^+\pi^+$ allow testing models with an extended Higgs sector and suppressed proton decay [28]. Within the context of supersymmetry, the di-nucleon decay mode $pp \to K^+K^+$ can provide the most sensitive experimental probe of the *R*-parity violating coupling λ''_{112} [29, 30]. Due to complicated systematics, associated with the final state mesons and their nuclear interactions, as well as the resulting convoluted multi-ring signatures, the analyses for the di-nucleon decays to mesons are done using a boosted decision tree (BDT) [31]. This allows one to get a far better discrimination between signal and background than by solely applying the event selection criteria. We illustrate this with a $pp \to K^+K^+$ search in SK-I [32].

Unlike $p \to \nu K^+$, the kaons in $pp \to K^+ K^+$ are above Cherenkov threshold and produce visible rings. Subsequently, the kaons decay, primarily through the $K^+ \to \mu^+ \nu, \pi^+ \pi^0$ channels. The two resulting kaon vertices are spatially separated by ~ 2 meters. After the pre-selection criteria have been applied, the remaining events are processed with BDT. The final BDT output is displayed in Figure 4. The cut on the final BDT output variable is chosen at 0.12, maximizing the (Sig./ $\sqrt{\text{Sig.} + \text{Bkg.}}$) ratio. Events to the right of the cut are taken to be signal candidates. With (without) BDT, one achieves the final signal efficiency of 12.6% (21.9%) and an expected total SK-I background of 0.3 (33.9) events. The data is found to be consistent with background and a 90% C.L. lower lifetime limit of $1.7 \times 10^{32} \text{ yrs.}^d$ is placed. This lifetime limit can be translated [30] into a limit on the λ''_{112} SUSY *R*-parity violating coupling, resulting in $|\lambda''_{112}| < 7.8 \times 10^{-9}$ [32].

^{*c*}This result can be converted into a limit for $n - \overline{n}$ oscillations in vacuum, yielding lifetime of around 10⁸ s. ^{*d*}The lifetime limits for di-nucleon decays are calculated per ¹⁶O nucleus.



Figure 4 – Final output of the boosted decision tree for $pp \to K^+K^+$ search. Events to the right of the cut at 0.12 are considered signal candidates. From Ref. [32].

Similarly, no significant signal excesses are observed in the di-nucleon $np \to \pi^+\pi^0$, $nn \to \pi^0\pi^0$ and $pp \to \pi^+\pi^+$ decay searches, resulting in the 90% C.L. lower lifetime limits of around 10³² yrs. for all three modes [33].

3.5 Spectral Searches

Due to a large theoretical uncertainty in the nucleon decay predictions, it is important to study a variety of channels. Since e-like and μ -like single-ring atmospheric- ν background is well understood, an array of modes producing such signatures can be readily analyzed. These include $p \rightarrow (e^+, \mu^+)\nu\nu, p \rightarrow (e^+, \mu^+)X^e$, $np \rightarrow (e^+, \mu^+, \tau^+)\nu$ and $n \rightarrow \nu\gamma$ channels. The trilepton $p \rightarrow (e^+, \mu^+)\nu\nu$ decays can appear within Pati-Salam models, with some [34] predicting their lifetime to be around 10^{30-33} yrs.

The search for all these channels is performed by applying a spectral "pull-method" χ^2 fit [35] to the *e*-like and the μ -like single-ring momenta, after the event selection. Figure 5 displays the best-fit result for the atmospheric- ν background MC, data (273.4 kiloton-yrs exposure) and the 90% C.L. allowed amount of nucleon decay signal (×10) after the fit. For these searches, the average signal efficiency is ~ 95% for the *e*-like modes and ~ 80% for the μ -like modes, with the latter being lower due to the decay-electron detection efficiency ^f. With no significant excess observed in either search, 90% C.L. lower lifetime limits of around 10³² yrs. are placed on all of the above channels [36, 37].

4 Summary and Outlook

Baryon number violation is motivated by various theoretical considerations and can be tested by nucleon decay searches. Large underground water Cherenkov detectors are highly sensitive to nucleon decays. We have reported on results for an extensive array of nucleon decay searches carried out at the current state of the art WC experiment, Super-Kamiokande. No significant signal excess has been found in any of the analyzed channels. These results, which correspond to the world's best lifetime limits, are summarized in Table 1.

The majority of the limits are already in the 10^{32} yrs. range, signifying that even some of the more baroque types of theoretical models are constrained. The projected gadolinium dissolution in the SK detector will allow us to further reduce the nucleon decay background and thus improve on the search sensitivity. Future experiments, such as Hyper-Kamiokande and DUNE/LBNF, are expected to improve the presented results by up to an order of magnitude. Since the majority

^eHere, X denotes a massless and invisible particle.

 $[^]f{\rm The}$ decay-electron detection efficiency is improved in SK-IV by 20% compared to other SK periods, due to upgraded electronics.



Figure 5 – [top] Reconstructed momentum distribution, with the SK data (black dots) and the best-fit result for the atmospheric- ν background MC (solid line) displayed. The corresponding residuals are shown below, after the fitted background has been subtracted from the data. [bottom] The 90% confidence level allowed nucleon decay signal multiplied by 10 (hatched histograms), from the signal and background MC fit to data. All modes are shown (overlaid), with e-like channels on the left and μ -like channels on the right. From Ref. [36, 37].

of the nucleon lifetime predictions from the various theoretical models lie below the $\sim 10^{36}$ yrs. range, significant discovery potential is expected in the upcoming searches.

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Decay Mode	$ \Delta(B-L) $	$\tau/\mathcal{B} (90\% C.L.)$	Reference
$p \to e^+ \pi^0$	0	1.7×10^{34} yrs.	[22]
$p \to \mu^+ \pi^0$	0	7.8×10^{33} yrs.	[22]
$p \rightarrow \nu K^+$	$0(\overline{\nu}), 2(\nu)$	6.6×10^{33} yrs.	[25]
$p \to \mu^+ K^0$	$0(\overline{\nu}), 2(\nu)$	6.6×10^{33} yrs.	[23]
$p \rightarrow e^+ \eta$	0	4.2×10^{33} yrs.	[13]
$p \to \mu^+ \eta$	0	1.3×10^{33} yrs.	[13]
$p \to e^+ \rho^0$	0	7.1×10^{32} yrs.	[13]
$p \to \mu^+ \rho^0$	0	1.6×10^{32} yrs.	[13]
$p \to e^+ \omega^0$	0	3.2×10^{32} yrs.	[13]
$p \rightarrow \mu^+ \omega^0$	0	7.8×10^{32} yrs.	[13]
$p \rightarrow \nu \pi^+$	$0(\overline{\nu}), 2(\nu)$	3.9×10^{32} yrs.	[38]
$p \to e^+ \nu \nu$	$0(\overline{\nu}\nu), 2(\nu\nu, \overline{\nu}\overline{\nu})$	1.7×10^{32} yrs.	[36]
$p \to \mu^+ \nu \nu$	$0(\overline{\nu}\nu), 2(\nu\nu, \overline{\nu}\overline{\nu})$	2.2×10^{32} yrs.	[36]
$p \to e^+ X^{\rm a}$	0(X?)	7.9×10^{32} yrs.	[37]
$p \to \mu^+ X^{\mathrm{a}}$	0(X?)	4.1×10^{32} yrs.	[37]
$n \rightarrow e^+ \pi^-$	0	2.0×10^{33} yrs.	[13]
$n \rightarrow \mu^+ \pi^-$	0	1.0×10^{33} yrs.	[13]
$n \rightarrow e^+ \rho^-$	0	7.0×10^{31} yrs.	[13]
$n \to \mu^+ \rho^-$	0	3.6×10^{31} yrs.	[13]
$n \rightarrow \nu \pi^0$	$0(\overline{\nu}), 2(\nu)$	1.1×10^{33} yrs.	[38]
$n \rightarrow \nu \gamma$	$0(\overline{\nu}), 2(\nu)$	5.5×10^{32} yrs.	[37]
$pp \rightarrow K^+K^+$	2	$1.7 \times 10^{32} \text{ yrs.}^{b}$	[32]
$pp \to \pi^+ \pi^+$	2	$7.2 \times 10^{31} \text{ yrs.}^{\text{b}}$	[33]
$np \rightarrow e^+ \nu$	$0(\overline{\nu}), 2(\nu)$	$2.6 \times 10^{32} \text{ yrs.}^{b}$	[37]
$np \rightarrow \mu^+ \nu$	$0(\overline{\nu}), 2(\nu)$	$2.0 \times 10^{32} \text{ yrs.}^{b}$	[37]
$np \to \tau^+ \nu$	$0(\overline{\nu}), 2(\nu)$	$3.0 \times 10^{31} \text{ yrs.}^{b}$	[37]
$np \to \pi^+ \pi^0$	2	$1.7 \times 10^{32} \text{ yrs.}^{b}$	[33]
$nn \to \pi^0 \pi^0$	2	$4.0 \times 10^{32} \text{ yrs.}^{b}$	[33]
$n - \overline{n}$ oscillations	2	1.9×10^{32} yrs.	[27]

Table 1: Summary of Super-Kamiokande nucleon decay search results.

^a X denotes a single particle which is assumed to be massless and invisible. ^b The lifetime limits for di-nucleon decays are calculated per ¹⁶O nucleus.