# The systematics study of power law parameters of $\gamma$ -Band and comparison with ground state band for medium mass region

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#### Introduction

The energy levels of nuclei consist of various bands as lowest band -ground state band, for symmetrical rotation  $K^{\pi}=0^+\beta$ -band and for asymmetrical rotation  $K^{\pi}=2^+\gamma$ -band as well as other higher bands and non bands [1]. Several empirical energy expressions are used [2-8] to calculate the theoretical energies and compared with experimental data [9]. The well known energy expression for rotational spectra:

$$E = \frac{\hbar^2}{2\theta} I(I+1) . \tag{1}$$

Where,  $\theta$  and I are the moment of inertia and spin, respectively. The Bohr Mottelson energy expression for deformed nuclei is:

$$E(I) = AX + BX^{2} + CX^{3} + \cdots$$
 (2)

Where, X = I(I+1), as a series expansions of the spin. For harmonic vibrator, the energy can be expressed as:

$$E(I) = aI . (3)$$

Das et al. [2] suggested the energy expression for an-harmonic vibrator: E(I) = aI + bI(I - 2) (4)

For the transitional-medium mass region A=150-200 Gupta et al. [3] proposed a single term expression for ground state energy as:  $E = al^{b}$ . (5)

Where, a, b and I are scaling coefficient, power index parameter and spin, respectively. The single term expression is used for low mass region by Mittal et al. [4]. For ground state band, in both regions, the index and coefficient are fairly constant and are independent of level spin. Kumar et al. [5] showed the correlation of kinetic moment inertia with power formula index in  $100 \le A$  $\le 150$  mass region. Also Gupta and Hamilton [6] illustrated the use of this formula to determine the degree of deformation of shape transitional nuclei.

Due to simple interpretation of this expression, it is used here for  $\gamma$ -band by subtracting band head difference as suggested by Gupta et al. [7]. The energy levels for this band were obtained by Gupta [8]. Here, the coefficients and indices of the different spins are obtained using equation (5) after subtracting band head difference E(2<sup>+</sup><sub>2</sub>). The 'a' and 'b' parameters of  $\gamma$ -band and ground band nuclei are compared for<sup>156</sup>Gd, <sup>156,162-164</sup>Dy, <sup>162-170</sup>Er, <sup>178</sup>Hf and <sup>186</sup>Pt. These nuclei are having the energies in  $\gamma$ -band up to spin I<sup> $\pi$ </sup> = 10<sup>+</sup>.

### Results

The scaling parameter 'a' and power index 'b' of  $\gamma$ -band and ground band are spin independent (see Fig. 1 and Fig. 2). The behaviour of scaling parameter 'a' and power index 'b' for  $\gamma$ -band and g- band are similar [3].

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Fig. 1: The variation of scaling parameter 'a' versus spin for  $\gamma$ -band and g-band.



Fig. 2: The variation of power index parameter 'b' versus spin for  $\gamma$ -band and g- band.

## References

[1] A. Bohr and B. R. Mottelson, Nuclear Structure, Vol.-II (New York, 1975). [2] T. K. Das, R. M. Dreizler and A. Klein, Phys. Rev.C2 (1970) 632. [3] J. B. Gupta, A. K. Kavathekar and R. Sharma, Physica Scripta, 51, 316,1995. [4] H. M. Mittal, V. Devi and J. B. Gupta, Physica Scripta, 81, 015202, 2010. [5] Rajesh Kumar, V. Katoch, S. Sharma and J. B. Gupta, Int. J. Mod. Phys. E21, 1250082, 2012 [6] J. B. Gupta and J. H. Hamilton, Phys. Rev. **C83,** 064312, 2011. [7] J. B. Gupta, S. Sharma and Vikas Katoch, Pramana Journal of Physics, Vol.81, 75, 2013. [8] J. B. Gupta, sympnp.org/prodg. 59(2014) [9] www.nndc.bnl