Astronomy and astrophysics with gravitational waves in the Advanced Detector Era

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Abstract. With the advanced gravitational wave detectors coming on line in the next 5 years, we expect to make the first detections of gravitational waves from astrophysical sources, and study the properties of the waves themselves as tests of General Relativity. In addition, these gravitational waves will be powerful tools for the study of their astrophysical sources and source populations. They carry information that is quite complementary to what can be learned from electromagnetic or neutrino observations, probing the central gravitational engines that power the electromagnetic emissions. Preparations are being made to enable near-simultaneous observations of both gravitational wave and electromagnetic observations of transient sources, using low-latency search pipelines and rapid sky localization. We will review the many opportunities for multi-messenger astronomy and astrophysics with gravitational waves enabled by the advanced detectors, and the preparations that are being made to quickly and fully exploit them.

1. Introduction

In the coming years, advanced ground-based gravitational wave (GW) detectors will be coming online, observing the sky as a detection and analysis network. We refer to this as the Advanced Detector Era (ADE). The first detections, followed by a growing catalog of sources, will be a trove of astrophysical information about the properties of these extremely energetic systems. In this talk and paper, I briefly review some of the many ways that gravitational waves can inform us about those properties.

There are many promising sources for gravitational waves. Transient sources include binary mergers, core-collapse supernovae, magnetar flares, and pulsar glitches. Some of these are believed to be the progenitors of gamma ray bursts (GRBs) or soft gamma repeaters (SGRs). Long-lived sources include continuous waves from rapidly spinning neutron stars (see talks by Andrzej Krolak and Bruce Allen at this conference), and the stochastic background from the early universe. The scope of this discussion will be limited mainly to binary mergers, with brief mention of other transient sources; we will refer the reader to excellent talks on many of these other subjects by speakers at this conference.

2. The GW detector network in the advanced detector era

The initial detector era: The initial LIGO [1] and Virgo [2] detectors completed their science runs in 2007. The "enhanced" LIGO [3] and Virgo [2] detectors ended data taking in October

2010. As of summer 2011, the H2 detector at LIGO Hanford Observatory (LHO) and the L1 detector at LIGO Livingston Observatory (LLO) are dismantled in preparation for Advanced LIGO installation. The H1 Enhanced LIGO detector at LHO is conducting a squeezed vacuum experiment in Fall 2011, after which, it too will be dismantled. During summer 2011, the Virgo [2] and GEO-HF [4] detectors are taking science data. The Virgo detector will end observations in preparation for Advanced Virgo by the end of 2011.

The advanced detector era: The construction of the Advanced LIGO (aLIGO, [5]) detectors is around 50% complete, and installation has begun at LHO and LLO. Advanced LIGO construction will complete in 2014. Commissioning will commence, and first science runs are expected to commence in 2014–2015 at Hanford and Livingston. The Advanced Virgo detector [6] in Cascina, Italy and LCGT [7] in Japan will also come online in the same timescale; see the talk at this conference by Shinji Miyoki and Kazuaki Kuroda. It should be kept in mind that it took several years for the initial LIGO detectors to achieve design sensitivity. The advanced detectors are far more complex, and although the commissioning team is far more experienced, it still may take substantial time to the advanced detectors to reach their design sensitivity. Note also that work is already in progress to design third-generation detectors which could improve sensitivity with respect to the coming advanced detectors, by as much as another fector of 10; see the talk at this conference by Harald Lück.

The third aLIGO detector: LIGO Laboratory is constructing three 4 km advanced detectors, two for installation at LHO and one at LLO. However, as discussed below, a far more powerful global detector network is possible if the third aLIGO detector is installed not in LHO but in a distant observatory site such as western Australia [8] or India [9]: see the talk at this conference by Kazuaki Kuroda. (Note that as of November 2011, the Australia option is no longer feasible due to lack of funding commitment from the Australian government).

The aLIGO strain noise spectrum: The advanced interferometric detectors are largely quantum noise limited over much of the detection band. they can be operated at high laser power (up to 125 watts) to reduce the shot noise at high frequencies (above 100 Hz) at the expense of increased radiation pressure noise below around 50 Hz; or vice versa at lower power. Furthermore, the advanced detectors feature a "signal cavity" at the asymmetric port of the interferometer (where the GW signal is extracted). When that cavity is tuned to the main laser carrier frequency, the detector operates in "broadband" mode. When detuned, it can improve sensitivity over some frequency band at the expense of others, so it can be optimized for binary neutron star signals or signals from higher mass binaries. Example anticipated aLIGO sensitivity curves can be found in Ref. [10].

The global network: The global advanced detector network includes the two LIGO detector sites, GEO-HF, Virgo, LCGT, and possibly LIGO-India. A detector network enables more confident detection by requiring the same or similar signal in widely separated detectors. More importantly, a network is required in order to locate the sources in the sky, since individual detectors have essentially no ability determine the source direction. Individual detectors are laser interferometers with quadrupole antenna patterns; a detector network acts as a gravitational-wave interferometer, determining source direction through timing and amplitude information of a wave detected coherently across a global baseline.

The need for a detector in Australia or India: The LIGO and Virgo detectors define a plane, and sky localization resolution is good for sources lying outside that plane, poor for sources near that plane. The addition of LCGT in Japan helps greatly, but that detector is also close to the same plane, now forming a larger triangle. The addition of a detector in Australia or India forms a global tetrahedron, with much improved resolution in all directions. To first order, LCGT improves East-West localization of the source, while LIGO-Australia or LIGO-India improves North-South localization. By coherently analyzing the data from all detectors as a single global network, one can improve sky localization accuracy to the level of a few square degrees over almost all of the sky. In addition, a distributed detector network with non-aligned antenna response patterns allows one to disentangle the two polarizations of the waves, from which one can measure the orientation of the source with respect to the detectors and thus the intrinsic amplitude of the waves at the source. This is crucial information for understanding the astrophysical properties of the source: the luminosity distance for standard sirens like binary systems; the GW energy release for core-collapse supernovae; or the non-sphericity of neutron stars emitting continuous waves. The message here is that the opportunity to relocate one LIGO detector in Australia or India will greatly enhance the scientific output of GW observations, especially for transient signals.

3. Astronomy and astrophysics with compact binary mergers

Good source localization allows one to look for other forms of radiation coming from that location, nearly simultaneously with the GWs: optical, radio, X-ray or gamma electromagnetic radiation, or neutrinos. Such multi-messenger signals may be expected from sources containing ordinary atomic or nuclear matter.

The dark side: However, GWs carry information about strong, rapidly changing gravitational fields, even if there is no ordinary matter present to emit other forms of radiation – what Kip Thorne calls "the dark side of the universe". A binary black hole inspiral, merger and ringdown may not be accompanied by any other form of detectable radiation. An isolated, rapidly spinning neutron star, even nearby, may not be observable in EM radiation. But the GW waveform itself carries a wealth of information about the system, much more than what can usually be obtained from EM observations alone.

Binary parameters: For a binary merger, this includes: the masses of the component objects; the orientation of the binary orbit with respect to the detectors (two angles); the sky coordinates of the system (two angles); the luminosity distance; and the time and phase of merger (as observed on the Earth) – a total of nine parameters. In general, the compact components of the binary (neutron stars and/or black holes) are spinning, and information about the magnitude and orientation of those two spin vectors is encoded in the waveform. For example, if the component objects have high spin, aligned with the orbital angular momentum, it will take more time and more gravitational wave cycles for the system to radiate away enough angular momentum in order to merge ("hang-up" and "spin-flips"). The six components of the component spins bring the number of parameters up to 15. If the orbit is eccentric, there are three more parameters; but by the time a binary orbit enters the frequency band of ground-based detectors, the extra radiation as the orbit passes through periastron effectively circularizes it.

It is rare for radiation from an astronomical object to carry so much information about the source. Electromagnetic radiation is typically generated from the incoherent motion of electrons in thermal or explosive events; gravitational radiation comes from the coherent motion of large (in LIGO's case, stellar-mass) objects.

Waveform models: Extracting this information requires accurate models of the source. For binaries, this is the relativistic gravitating two-body problem. In the early phases of the inspiral, the waveform is well understood in the context of the post-Newtonian expansion [11]. For the late stages of inspiral and merger, recent spectacular advances in numerical relativity [12] have provided waveforms for a range of binary parameters, and semi-analytical and phenomenological models have allowed us to interpolate (and even extrapolate) to cover the space of binary parameters.

Binary mass range: The parameter space is large: 9-dimensional if spin is neglected, or 15dimensional if it is included, as it needs to be. Component masses can range from $1 M_{\odot}$, through the typical neutron star mass range around $1.35 M_{\odot}$, and higher (where M_{\odot} is the solar mass). Compact objects with mass above $3 M_{\odot}$ are expected to be black holes. astrophysical black holes that form from core collapse of very massive stars are expected to be as massive as $20 M_{\odot}$

or more. Supermassive black holes with masses of $10^6 M_{\odot}$ are also known to exist; and it may be surmised that intermediate mass black holes with masses of $20 - 1000 M_{\odot}$ might also exist, perhaps formed via mergers of smaller black holes. Any and all of these may form binaries that may merge via gravitational radiation within the age of the universe.

Frequency at merger: Binaries with total mass M (in solar mass units) reach their innermost stable circular orbit before merger when the GW frequency reaches around 4000 Hz/M. Low mass systems (with total mass below around 5 M_{\odot}) merge at high frequencies outside of the most sensitive band of the advanced detectors (roughly 20 – 1000 Hz), while the merger of higher mass systems is in the most sensitive band. Above 100 M_{\odot} , only the last part of the waveform from the ringdown of the final merged black hole is in band. In the low mass case, post-Newtonian templates are sufficient to capture the signal; in the high mass case, damped sinusoids are suitable templates. In the intermediate case (total mass of 5 – 100 M_{\odot}), models [13, 14] that match the inspiral to the ringdown with a merger phase tuned to numerical relativity waveforms are needed. These latter waveforms do not yet include the effects of spin.

Sensitivity and rates: Using these models as templates for searches, one can estimate the sensitivity of the advanced detectors to binary mergers as a function of distance and total mass. Experience from the initial LIGO-Virgo observations suggests that reliable detection is possible with an average SNR per detector of around 8. Averaging over binary sky location and orbital orientation, the aLIGO detector can register a signal with SNR of 8 or more from a binary neutron star merger to a distance of around 200 Mpc, and from a binary black hole system (with component masses of 10 M_{\odot} each) to a distance of almost 1000 Mpc [15]. For all masses of interest, the sensitive distance is sufficient to expect that the density of sources (galaxy mass or luminosity) per unit volume is uniform and constant (roughly 0.01 Milky Way Equivalent Galaxies per Mpc³) [15, 16]. Using population synthesis models anchored to the handful of observed binary neutron stars in the Milky Way, this leads to predicted detection rates in the advanced detector era of around 40 binary neutron star mergers and 20 binary black hole mergers per year (with errors of a factor 10 or more in both directions) [15].

Parameter estimation: Once binary merger events are observed, it is possible to extract their parameters. In practice, the signals will be buried in noisy detector data, so the data from all detectors in the network are filtered through a coherent set of model waveforms ("templates"), which depend in known ways on the parameters enumerated above, and a network SNR is computed. One explores the parameter space to maximize the SNR with respect to the parameters. But because the parameter space is so large, some efficient algorithm is employed, such as Markov Chain Monte Carlo [17] (MCMC) or nested sampling [18]. Even then, these calculations are computationally demanding; Parameter estimation on hardware injections in the 2009–2010 LIGO-Virgo observations took many days per event on clusters of computers. Work is in progress to speed up these computations dramatically.

Parameter accuracy: The waveform carries information about both component masses, but the phase evolution of the waveform depends to first order only on the combination known as the chirp mass $\mathcal{M} \equiv M_{tot}\eta^{3/5}$, where $M_{tot} = m_1 + m_2$ is the total mass and $\eta = m_1 m_2/M_{tot}^2$ is the dimensionless symmetric mass ratio. The chirp mass is well measured, while η is measured relatively poorly, leading to a measurement confidence band in m_1 , m_2 parameter space. Experience from hardware injections in the 2009–2010 LIGO-Virgo observations inform us that the mass accuracy depends strongly on the waveform accuracy (eg, one gets different results from 2.5-order and 3.5-order post-Newtonian waveforms) [19]. The dependence on spin is weaker.

Sky position: As discussed above, the ability to measure sky position of the source depends greatly on the number and location of detectors in the network, as well as on the type of waveform (frequency content) and, of course, the SNR. Burst events near detection threshold in the initial detector network can have 90% confidence level localization area of more than 100

square degrees, typically in multiple disjoint regions and arcs across the sky [20]. Even in the best of circumstances (high SNR for a 1 kHz signal in many advanced detectors), sky localization is diffraction limited at not much better than a square degree [21, 22, 23, 24]

Luminosity distance: Gravitational waves from binary inspiral are "standard sirens" [25], making them useful tools for measuring the Hubble constant in the local universe (redshift $z \approx 0$) with very different (and potentially small) systematic errors with respect to measurements using standard candles like Type 1a supernovae. Their amplitude at the detector depends on the luminosity distance to the source, but also on the sky position and orbit orientation; there is a strong degeneracy between the luminosity distance and the inclination ι of the orbit with respect to our line-of-sight. The orbit orientation can be measured using a network of detectors with different sensitivities to the two GW polarizations (plus + and cross ×), since these depend differently on cos ι . In the best of circumstances (high SNR in many non-aligned detectors), achieving 1% resolution on luminosity distance requires the detectors' amplitude calibration uncertainty to be of the same order [25, 26]. In Enhanced LIGO, the detectors' calibration uncertainty was more like 10%, but improvements are expected for aLIGO.

Component Spins: Waveforms from binaries with massive spinning components will be modulated in phase and amplitude. The orbital angular momentum L will precess around the total J = L + S, modulating the orientation of the orbital plane; and thus the amplitude at the detector. The frequency evolution will also be modified (see discussion of orbital hang-up, above). By making use of a sufficiently accurate waveform model, one can estimate the two 3-dimensional spin vectors (relative to the total or orbital angular momentum) from the observed waveforms. Much effort is going into the development of the waveform models that incorporate spin, as well as the parameter estimation codes that explore spin parameter space with post-Newtonian waveforms [27].

Tidal disruption of neutron stars in merging binaries: The GW waveforms from compact binaries deviate from the point-particle limit as the objects approach merger. For binary black holes, this is in principle computable in numerical relativity from the equations of General Relativity. If one or both of the compact objects are neutron stars, they will become tidally disrupted near merger, severely distorting the waveform at high frequencies (for binary neutron stars, above around 500 Hz). This is a complicated process, involving not just strong field highlydynamical gravity, but also nuclear physics, magnetic fields, and the formation of an accretion disk; the first simulations are now in hand [28]. To lowest order, however, the frequency at which the distortion sets in is governed by the size (compactness) of the neutron star. This in turn depends on the microscopic laws governing the equation of state (relation between pressure and density, or compressibility) of nuclear matter in the stars; properties of great interest to physicists interested in nuclear matter at the extreme conditions of neutron stars. "Soft" equations of state result in more compressible matter and thus more compact stars, which disrupt at tighter orbits (higher frequencies); "hard" equations of state are the opposite. Since advanced detectors have noise curves that get worse at frequencies of 500 Hz and above, much effort is going into improving detector sensitivity at higher frequencies, and in measuring the neutron star compactness at the lowest frequencies that can carry that information [29].

4. Multi-messenger astronomy

Complementary information: Energetic astrophysical systems involving ordinary or nuclear matter will emit both gravitational and electromagnetic radiation over a wide range of wavelengths, all carrying different and valuable information about the source. Gravitational waves tell us about the bulk motion dynamics such as binary parameters. The GW energetics are a direct probe of the central engine powering the energy release. And they can be used as standard sirens to measure luminosity distance for cosmology. The spectrum and multi-wavelength light curve of the electromagnetic radiation gives us the precise sky location, so that

we can identify the host galaxy and galaxy's redshift. The EM afterglow energetics allow us to probe the nature of the progenitor star and its gas environment. Coincident information from GW and EM observations thus provide a much more complete picture of the progenitor astrophysics. Combining these observations will also greatly increase the confidence in the detection above the detector background.

The flow of information – EM triggers: EM events can trigger deeper (offline) searches of the GW detector data. GRBs or SGR flares detected from very wide-field space-based X-ray and gamma ray telescopes give a precise time and sky location of the event; this permits a targeted search for coincident GW signals (in data "in the can"), reducing the noise contamination in GW detector network with respect to all-sky, all-time searches. detection thresholds can be set lower, allowing for deeper searches.

The flow of information – GW triggers: The GW detector network is sensitive to signals from (more-or-less) the whole sky, at all times (modulo the detectors' operational duty cycle). By contrast, ground- and space-based optical and radio telescopes need to know where to point. Low latency GRB alerts have allowed for the discovery of optical afterglows, greatly increasing our information about the sources. Similarly, low latency GW alerts can serve a similar function in the cases where there is no prompt GRB, either because it is not beamed towards us or is absent from the source. GW emission cannot be beamed strongly, as GRBs are believed to be. But to catch the prompt EM afterglow, GW triggers must be generated and broadcast, and telescopes must be pointed, quickly. Afterglows can fade on the timescale of hours, or even minutes. Because GW sky localization is poor, even very wide-field (of order 10 square degree) optical telescopes may need to take many images (over many days) to observe the sky region consistent with a GW signal, in the hope of finding a possible EM counterpart. This requires development of low-latency GW detection and sky localization pipelines, protocols to pass info, telescope scanning strategies and, ideally, coordination of EM observations amongst different telescopes.

The flow of information – GW detections and all-sky telescopes: GW detectors see the whole sky and can store all the data indefinitely. So can neutrino detectors like ANTARES and Ice-Cube. Present and future large-scale optical and radio transient surveys are also rich repositories of potential multi-messenger sources with data "in the can". Searches for events near-coincident in time and space can be done offline, through "data mining".

Enabling the flow: Prototypes for all of these paths have been developed; see talks at this conference by Marica Branchisi and Irene Di Palma. But they need to be fully tested, flawless and ready when the advanced detector network comes online in the next few years. Online, low latency GW search pipelines will identify potential GW detection candidates within ~ 1 minute of data taking. They will estimate and broadcast their time, sky location with a sky probability map, false alarm rate, and other relevant info like binary masses, frequency band, etc. Information about confirmed detections will take longer (maybe months at first), and will include all of the above, plus snippets of the strain data h(t), noise spectral densities of the detectors at the time of detection, improved parameter estimation, etc. These will be assembled into a catalog of transient detections to enable queries of the population distribution in terms of any and all measured parameters.

Besides for binary mergers, astrophysical sources of high energy photons that may also have associated GW bursts include gamma ray bursts (GRBs), core-collapse supernovae, magnetars and pulsar glitches. Searches for gravitational wave bursts from these sources are discussed at this conference by Laura Cadonati and Giovanni Prodi.

Short-hard GRBs: Joint GW and EM observations of short hard GRBs detected by spacebased gamma ray telescopes can confirm (or rule out) the merger progenitor model; permit the study of the progenitor systems, including orientation and GRB beaming; relate the GW and EM energy release to test detailed models; and relate merger parameters to hosts (metallicity,

star formation rate, etc.) to test population synthesis models. As mentioned above, such events can be used to make an independent, self-calibrating measurement of the Hubble constant at low redshift (since high redshift GWs from mergers will not be detectable by the coming advanced detector network). Coincident detection of high energy neutrinos produced in the internal shock of the GRB progenitor explosion will be a spectacular discovery.

Long-soft GRBs: Joint GW and EM observations of long GRBs can test progenitor models such as the Collapsar model (core collapse of a massive, rapidly spinning and highly magnetized star). The GRB is known to be strongly beamed. The GW burst will not be strongly beamed, but may be too weak to be detected at large distances (10 Mpc or more), and the waveforms are poorly modeled. If the source is sufficiently close, the copious low energy neutrinos may be detectable.

Core-collapse supernovae: Typical core-collapse supernovae will be observable in GW bursts for progenitor stars in our Galaxy; extra-galactic supernovae will produce detectable GWs only in the most extreme models [30]. Unfortunately, the rate of core-collapse supernovae in our Galaxy is small, of order 1 in 50 years. The GW burst is from the core collapse itself, while the supernovae light (detectable from even very distant galaxies, but possibly obscured by dust for supernovae in our Galaxy) appears only when the shock breaks out to the surface of the progenitor star, hours later. The observation of the GW burst provides extremely valuable information about the details of the core collapse and subsequent shock as it propagates through the outer stellar material. The huge energy release of low-energy neutrinos (detectable from supernovae in our local group of galaxies) provide more valuable information about how the shock propagates and breaks out.

Magnetars: Highly magnetized neutron stars $(B \sim 10^{15} G)$ are observed as Soft Gamma Repeaters (SGRs) and Anomalous X-ray pulsars (AXPs) On the order of 20 are known in our Galaxy. They emit short bursts of X-rays and soft gamma-rays ($\sim 10^{42}$ erg), sometimes giant flares $(10^{44} - 10^{46} \text{ erg})$ or storms of bursts, and QPOs in the giant flare tails (10 - 2000 Hz). The energy release may excite neutron star crustal f-modes in the kHz region, ringing down by GW emission, but with unknown energy. Torsional (shear) s-mode "core-quakes" may release significantly more GW energy. Searches with initial detector data [31] yielded limits on GW energy emission significantly higher than EM emission $(10^{48} - 10^{50} \text{ erg})$. We can expect a factor 100 better sensitivity (in emitted energy) with advanced detectors; and hope to get lucky with a nearby magnetar burst.

Pulsar Glitches: Pulsar glitches may be caused by star-quakes, or the sudden transfer of angular momentum from a superfluid core to a solid crust. These energetic events may excite quasi-normal mode oscillations in the neutron star interior, coupling to GW emission. An Initial LIGO search for GW ringdown signals (1–3 kHz) from a Vela pulsar glitch in 2006 [32] yielded upper limits in the range of $10^{44} - 10^{46}$ erg. Many more pulsars will be discovered and monitored in the coming years with LOFAR and SKA. Nearby, glitchy ones will be promising candidates for coincident GW emission detectable by the advanced detector network.

5. Summary and conclusions

Gravitational wave transients from extremely energetic astrophysical events are a rich trove of information about the progenitor system, both on their own and in coincidence with information from gamma ray, X-ray, optical, radio, and/or neutrino emission.

We look forward to the coming advanced detector era: the discovery and exploration of the GW sky, joint observations and discoveries with EM and neutrino telescopes, and the emergence of a rich new branch of astrophysics.

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