NOTES ON THE KALUZA-KLEIN PROPOSAL AND ELECTRO-NUCLEAR GRAVITY (Report to the Leipzig Conference on High Energy Physics, July 1984)

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I. INTRODUCTION

To my mind there is no question but that the revival of the Kaluza-Klein proposal (first made 65 years ago) represents the most exciting idea introduced into particle physics after supersymmetry and supergravity. Its importance lies, not so much in the electro-nuclear-gravity unification: it is rather that this proposal provides the only way in which the mysterious internal symmetries of particle physics can be given a physical meaning.

In this brief re-count, I discuss (1) The role of Kaluza-Klein cosmology as a window on extra dimensions; (2) Achieving of spontaneous compactification, with perturbative stability (no tachyons); (3) Realistic electro-nuclear-gravity symmetry, either for quarks and leptons or for preons; (4) Chirality of fermions and (5) Prospects of Super-Kaluza-Klein (SKK).

II. NECESSITY OF INTRODUCING BOSONIC MATTER FOR SPONTANEOUS CLASSICAL COMPACTIFICATION AND SUPER-KALUZA-KLEIN (SSK) THEORIES

Minimal (and according to Weinberg, "conservative") K-K theory in d-dim. is given by: L = $L_{Einstein} + L_{fermions}$.

With this Lagrangian, since $R_{MN} = T_{MN}(\Psi) + g_{MN}(T+\lambda)/(2-\dot{\alpha})$ and since $\langle \psi \rangle = 0$, compactification criteria of Eq.(A.1) of the Appendix ($C_1 \leq 0, C_2 > 0$) cannot be met (except for $C_1 = 0 = C_2$, i.e. Minkowski x ($S_1 \ge S_1 \ge S_1 \ge \ldots$) compactification with no non-Abelian symmetries). Thus we need either (1) <u>Dynamical compactification</u> through Fermi condensates $\langle \bar{\psi} \psi \rangle \neq 0$; or (2) <u>Radiatively induced compactification</u>, i.e. computation of the effective action radiatively. Examples are, for odd d (dimensionally-regularized), finite one-loop computation of P_{MN} with internal fermion lines, by Candelas and Weinberg [1] and

with internal gravitional lines, by Sarmadi ^{*)} [2a] and by Chodos ^{*)} [3], or (3) <u>Classical compactification</u>, i.e. introduce extra bosonic matter fields, e.g. (a) vector fields A_{M} [4] or (b) antisymmetric fields A_{MNP} [5,6] or (c) scalar fields, e.g. non-linear σ -model [7,8].

One method to reduce arbitrariness of introducing such basic matter fields - is to consider ungauged or gauged supergravity theories which from their very construction contain fields of the type A_M , A_{MNP} or σ . The ideal K-K theory would, therefore, be Super-Kaluza-Klein - SKK - (i.e. extended supergravity for $d \leq 11$), without extra matter multiplets. A second (in general non super-symmetric) method is to think of 2 stages of a theory which starts with $L_{Einstein} + L_{Fermi}$ in D dimensions. With the fermions present one may imagine that a radiative compactification [1] to d-dimensions $M^d \times G/H$ has been achieved, where dim G/H = D - d. At this stage a consistent <u>effective</u> Lagrangian may emerge in (the lower) d-dimensions, which contains massless fields only with $L_{Einstein}$ (in d-dimensions) plus L_{YM} (based on G) plus minimally coupled fermions. With either approach adopted, to illustrate the further problems of <u>compactification</u>, <u>stability</u> and <u>chirality</u>, in the sequel we consider theories with $L = L_{Einstein} + L_{YM} + L_{Fermi}$ (i.e. minimally gauged spin 1/2 fermions) + λ will be fine-tuned to give <u>Minkowski</u> compactification (in general one finds $\lambda \sim G^{-1}a^{-2} \sim \alpha G^2$). But before this, consider the cosmological aspects of KK.

III. KALUZA-KLEIN COSMOLOGY AS A WINDOW ON HIGHER DIMENSIONS

The best tests of K-K ideas (at present) appear to come from early universe cosmology:

(1) Variation with time of the fine structure constant α and the Newtonian constant G

W. Marciano [9] has given the following empirical limits on variation of α and G:

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  \dot{G}/G < 1 \times 10^{-11} \text{ yrs}^{-1} \quad (\text{Astrophysics}) \\   \dot{\alpha}/\alpha < 1 \times 10^{-17} \text{ yrs}^{-1} \quad (\text{Geochemical}) \\   \dot{\alpha}/\alpha < 4 \times 10^{-12} \text{ yrs}^{-1} \quad (\text{Laboratory; Astrophysics})
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*) These off-shell computations of effective action are necessarily gauge dependent; even the minimum of the potential appears to be so.Randjbar-Daemi and Sarmadi [2b] working in the light-cone gauge, (with no manifest Lorentz-invariance) obtained no compactification up to d=21. Chodos [3] working in a relativistic gauge showed that the theory has tachyons. Ignoring their contribution he finds compactification $(C_2 > 0)$ for d=17. (Sarmadi has confirmed the results of Chodos [2a].) Clearly we do not yet know if this problem (of gauge dependence) is a fundamental problem or an avoidable technicality, (see in this connection Ref.[2b].

In general, in KK theories α (M_{KK}) = k G/a² and G = \overline{G}/a^{d-4} (where \overline{G} is the constant which occurs in the Lagrangian for d-dimensions); thus $\dot{\alpha}/\alpha$ (M_{KK}) = (2-d) \dot{a}/a if $\dot{k} = 0$. If future experiments uphold this, the (near) constancy of G and α (more precisely of $\alpha(0)$, which is related to $\alpha(M_{vv})$ through renormalization group relations) may be traced to $\dot{a} \gtrsim 0$.

(2) <u>Near constancy of the internal radius ($\dot{a} \approx 0$)</u>

Do cosmological solutions of KK equations exist - which after a certain epoch - or equivalently below a certain temperature - give a (near constant) internal radius a(t) with the external (4 space-time) radius R(t) of the standard Friedmann-Robertson-Walker type?

The answer appears to be, yes. Randjbar-Daemi, Salam and Strathdee [10] (hereafter referred to as RSS) find $\dot{a} = 0$, $R^2(t) = t(t_0-t)$ as <u>exact</u> solutions of KK equations, for temperatures $T < \frac{1}{a}$, with a scalar-matter one-loop potential. The stability of this type of solution has been (positively) examined by Bailin, Love and Vayomakis [11]. Earlier, Ramond [12]had motivated a similar result for Zeldovich Cosmology ($p = \rho$). Subsequently a number of configurations of matter density, (including SKK) have been shown to lead to $\dot{a} \approx 0$ [13].

(3) Inflation from collapse of KK integral dimensions

A beautiful idea of motivating inflation in a KK context from the collapse of the internal dimensions has been suggested by several authors [14,11]. Three mechanisms have been considered. One idea is to assume that the total entropy in a co-moving volume remains constant; i.e. $R \sim a^{(4-d)/3} T^{(1-d)/3}$. Thus a modest decrease in "a" (the internal radius) and in temperature. T, may produce a large increase in R (by a factor of $\sim 10^{28}$ or more) if d is large ≈ 100 . How exactly the decrease in "a" comes about is a

dynamical question as is the reheating of the universe close to the original temperature. Shafi and Wetterich [14] (in a different approach) use non-minimal d-dimensional gravity R^2 terms); they show that a causal domain of the early universe gets trapped in a de-Sitter phase long enough for sufficient inflation to occur. Yoshimura[14], in a still different approach, considers the possibility, in KK context, that the universe may bounce in a closed model, and it may eventually, after some cycles of expansion and contraction, be driven into a nearly flat universe. In each cycle, presumably there are some kind of dissipative processes and entropy produced in each cycle may accumulate. Yoshimura shows that higher dimensional gravity quantum effects may provide the source mechanism, (see, however, Bludman, Guth and Sher [15]).

(4) Problem of dark remnants of the KK spectrum

Kolb and Slansky[16]have raised the problem of dark remnants of the KK spectrum; the problem is particularly severe in some KK models, e.g. the unrealist d=5, where the KK spectrum consists of charged massive particles ($M_{\rm KK} = n M_{\rm Planck}$) which cannot decay into the lowest (zero mass) excitations (gravitons, photons, Brans-Dicke scalars). Thus if, at present, $n_{\rm KK} \approx n_{\gamma}$, then $M_{\rm KK}$ must not exceed $\approx 100 \, {\rm ev}$, if the universe is not to be swamped by the KK density. Any stable KK particles must therefore annihilate with their antiparticles. Even so, Kolb and Slansky,with reasonable assumptions, estimate that $M_{\rm KK}$ must be less than $10^6 \, {\rm GeV}$. The problem is similar to the monopole abundance problem, only much worse. Kolb and Slansky suggest a number of ways out; e.g. (1) the internal radius a $\sim \frac{1}{M_{\rm KK}}$ may have been larger than $10^6 \, {\rm (GeV})^{-1}$ at early times, (see Ref.[17])shrinking later to its present value $\sim \frac{1}{m_{\rm Planck}}$; (2) Alternatively, the present entropy may have been created <u>after</u> compactification (see Koikawa and Yoshimura [14], who suggest a damped oscillation mechanism around compactified "a "of $\approx 10^{40} \, {\rm sec}^{-1}$ which can produce energetic particles which later thermalize). In any case, this mystery (of the missing stable KK spectrum) will place important restrictions on the type of acceptable KK theory.

(5) <u>Magnetic monopoles in higher dimensions</u>

Finally, several authors [18] have considered the problem of magnetic monopoles in KK theory. Ezawa and Iwasaki [18] show that for d=5 the Hamiltonian is hermitean in each charge - suggesting that the Rubakov-Callan effect may not occur in d=5.

IV. RESTRICTIONS ON DIMENSIONALITY OF SPACE-TIME (d) AND ON MODELS OF ELECTRO-NUCLEAR-GRAVITY

Restriction from anomalies

(1) Anomalies lead to a breakdown of gauge invariance, and thereby to breakdown of unitarity. They must be exorcised irrespective of the issue of renormalization. This has important bearings on the possible value of dimensionality parameter d and on possible models of electro-nuclear-gravity.

(2) Since Weyl-fermions exist only for <u>even</u> d, <u>odd</u> d theories are anomaly free.

(3) Three types of anomalies are known (a) Pure gauge (non-Abelian or U(1);(b) Mixed gauge and gravitational and (c) Pure gravitational.

Types (a) and (b) are well known from d=4 and exist for all even d. Type (c), pure gravitational anomalies were first discovered by Alvarez-Gaumé and Witten [19]. They may be of Einstein or Lorentz varieties [20]; the equivalence of these two types has recently been shown by Bardeen and Zumino[21]. These anomalies exist for $d = 2, 6, 10, \ldots$; graphs with internal self-dual antisymmetric tensor fields also being anomalous.

(4) All anomalies are proportional to Sym. Trace $(\lambda^a \lambda^b \dots \lambda^p)$ (p = d/2 + 1, d/2 - 1,...) where λ 's are the appropriate internal symmetry matrices. Right fermions anomalize oppositely to left fermions, likewise for self-dual and antiself-dual tensors.

(5) Clearly for d = 2,6,10,... there is no hope of anomaly safe groups (p=d/2+1) even). For d = 4,8,... however, there do exist safe groups for non-Abelian gauge anomalies: e.g. SU(2); G_2 ; F_4 ; E_7 ; E_8 ; SO(2q+1), $q \ge 2$; (Sp(q), SO(2q), $q \ge 4$, q even) and (Sp(q), SO(2q), q odd, if $d/2 \le q - 3$)). E_6 is anomaly free for d=4 (see Ref.[22]). (Note SO(10) is not safe for d=8.)

(6) Mixtures of left and right antisymmetric representations of spin-1/2 fermions for SU(N) groups have been examined by Frampton and Kephart[23] for possible anomaly cancellations. For each N, there are 1/2 (N - d/2 - 1) independent combinations of anti-symmetric representations of SU(N), (e.g. $6_L + \delta_L + 15_R + 15_R + 20_L$ is anomaly-free for SU(6) for d=6); these mixtures are most simply classified in terms of representations of super-algebras SU(N/M) with M satisfying N - d/2 - 1 > M [24a]. Since $\frac{1}{2}$ (N - d/2 - 1) > 1, this places a lower limit, N > 6 for d=6 (this excludes SU(5)); N > 7 for d=8 and N > 8 for d=10, for this class of toally antisymmetric representations.

(7) For d=6, Alvarez-Gaumé and Witten [19] show that a mixture of one "spin 3/2" 21"spin 1/2"and 8 self-dual tensors gives a gravitational anomaly-free theory. For d=10, there is one unique anomaly free theory, the N=2, chiral d=10 Super-Kaluza-Klein theory. For d > 10, there is no possibility of cancelling the gravitational anomaly with any mixtures of 3/2,1/2 and A multiplets [24b].

V. COMPACTIFICATION, STABILITY AND CHIRALITY FROM MINIMAL GAUGING

Minimally coupled gauge vector fields in higher dimension (SKK) theories are favourable for compactification, stability and chirality, after descent to d=4.

(1) Percacci and Randjbar-Daemi [25] have shown that a theory with $G_{YM} = H$ and $L = L_{Einstein} + L_{YM} + \lambda$ (considered either as an approximation to SKK or arising as L_{eff} from a still higher-dimensional KK) compactifies on (Minkowski)^L x G/H with

 $<A> = L^{-1}(y)dL(y)\Big|_{H}^{'}$ where L(y) is a map from G/H into G; $L^{-1}dL\Big|_{H}$ is the spin connection for <u>symmetric</u> spaces G/H. RSS [26] and Schellenkens [27 have shown that for $G_{YM} \subseteq H$, the compactified theory is perturbatively stable (tachyon-free). If, however, $G_{YM} \supset H$, stability depends on the type of embedding of H in G_{YM} .

(2) Even if we start in higher (even) dimensions with left (or right) Weyl fermions, descent to lower d, in general, would produce vector-like theories. However, with minimal gauging <u>only</u>, backgrounds of the PR type (on account of their topological properties) can give rise to chiral fermions in d=4 (RSS, in preparation). In Tables I, II and III we examine this for d = 6,8,10.

(3) The final gauge-symmetry is $G \ge G' \ge G_{YM}$. One will obtain different types of models depending, for example, on whether is G or G' which is identified with the electro-nuclear or with the family symmetry.

To summarize, d=8 (with instanton compactification) is the safest dimensio: [33a,33b,34a,34b]. A realistic model can be built (with three SU(5) families) or with families of SO(10) with an appropriate G_{YM} (see [33],[34],[36] and [37]). The gauge group G_{YM} is restricted by anomaly, stability and chirality considerations, but is otherwise arbitrary. In the next section we consider Super-Kaluza-Klein models for restricting this arbitrariness. Unsolved, at present, is the problem of breaking of the gauge symmetries.

VI. ELECTRO-NUCLEAR-GRAVITY MODELS FROM SUPER-KALUZA-KLEIN (SKK) THEORIES

The models considered fall into two classes:

(1) Quark-lepton models: here the emergence of at least 3 families of massless guarks and leptons after compactification to d=4 and fermion chirality present two of the outstanding problems.

(2) Preonic models.

Quark-lepton models

Of the two inequivalent pure supergravity <u>maximal</u> models, i.e. d=ll, N=l and d=l0, N=2 chiral, the quark-lepton content of neither one appears to resolv the first problem. Quarks and leptons, if fundamental objects, must therefore be introduced in SKK as extra "matter". This, together with chirality considerations appear to limit the choices to the following cases:

(1) d=10, N=1; with quarks and leptons in (the adjoint representation of a Yang-Mills) vector multiplet. This model cannot be compactified to d=4, unless radiative corrections produce a desidered compactifying potential [36].

The Yang-Mills group of choice is E_8 - the only group with the remarkable properties that (1) its adjoint representation is also the fundamental. (2) E_8 can descend to SU(5) through the chain $E_8 + E_7 + E_6 + SO(10) + SU(5)$ [37].

(2) d=8, N=1 with quarks and leptons again in the N=1 vector multiplet; an SU(2) gauged version of d=8, N=2 theory (descending from d=11, N=1) has recently been constructed [38].

The theory can be compactified to d=4 in various ways(with or without instantons) All compactifications lead to $(AdS)^4$. Chiral fermions may emerge when composite gauging of a further SU(2) x U(1) (present in the theory) is taken into account. Whether chirality will survive the compactification to d=4, still needs to be examined.

(3) Gauged chiral d=6, N=2 with monopole compactification [39,40,41]. Notwithstanding the presence of anomalies this offers the best model, at present, for quark and lepton matter. The model starts with chiral supergravity, plus N=2 hyper-multiplets, (content: spin 1/2 and zero, only). Why hyper-multiplets are to be introduced in a pure SKK content is of course not clear. However, once they are introduced, they are not arbitrary. These hyper-multiplets must be non-linear (S/R) Kähler-quaternionic according to a result of Bagger and Witten [42]; that is S/R can ony take the forms shown in Table IV with the fermionic content displayed according to the representation of R. Note7all fermions are singlets of Sp(1). Nishino and Sezgin [39] have shown that super-symmetric minimal gauging can be carried out for all the stability groups R (or any subgroups thereof). We are thus dealing in d=6 with N=2, chiral supergravity, with chiral fermions <u>of a specific content</u>, <u>minimally gauged</u>.

The next task is of compactifying from d = 6 to d = 4. Since we credealing with a gauged Yang-Mills theory, a U(1) subgroup of Sp(1) or of the remainder of R, should give rise to chiral monopole gauging. Except

for the case when $R = SU(n) \times U(1) \times Sp(1)$, where the monopole can be embedded in the U(1) factor of R, all other cases of embedding are unstable (Table I). To remedy this, one may either (A) concentrate on $\frac{SU(N,2)}{SU(N) \times U(1) \times Sp(1)}$ or (B) gauge only a subgroup of R which contains an explicit U(1) factor. For type (A) theories, consider N=16; the final symmetry group of the effective theory will be $SU(16) \times U(1) \times Sp(1) \times SU_{yy}(2)$ where the last $SU_{KK}(2)$ comes from the Kaluza-Klein side and can serve as the family group - the number of families equals the monopole charge |n| = 2q + 1, where q labels the $SU_{KK}(2)$ representation. Each family is a 16-fold of SU(16). An example of Type (B) theory is $E_{\gamma}/SO(12) \ge Sp(1)$, where only the SO(10) x U(1) subgroup of SO(12) is gauged. Here the final gauge symmetry is SO(10) x U(1) x Sp(2) x SU_{KK}(2), where again the SU_{KK}(2) is the Kaluza-Klein family group, with |n| = 2q + 1 families, each family containing a 16-fold of SO(10) [41]. A second example is the case of $E_8/E_7 \propto Sp(1)$, where $SO(10) \times U(1) \times U(1)$ subgroup of E_7 is gauged. In this case the 56 Majorana-Weyl decomposes to the (1 + 1 + 10 + 16) Weyl representation of SO(10).

Anomalies

All these theories are gravitationally anomalous in d=6, except for the case of $E_8/E_7 \times Sp(1)$; this is provided that the partial gauging is carried out only for the SU(3) x SU(2) x U(1) x $[U(1)]^4$ subgroup of $E_7 \times Sp(1)$. (This is to ensure that the gauge group has no more than 16 parameters^{*}), which is what is needed in the Alvarez-Gaumé-Witten anomaly cancellation condition [19] given that the hyperfermions are in the (Weyl) 27 of E_7 .) None of the models is free of gauge anomalies (at least a U(1) anomaly survives even for d=4). The anomaly problem is the most urgent to be solved for all such models.

To summarize d=6, N=2 provides the best candidate SKK electro-nucleargravity for quarks and leptons. Its characterizations are:

(1) In d=6, the model starts with chiral fermions; chirality is preserved for d=4 after monopole compactification.

(2) The theory compactifies on a Minkowski manifold; this is the only known theory with this property.

(3) The theory possesses two length scales; one related to Planck length, the other related to the expectation value of a scalar field in a manifestly Lorentz-invariant formulation of the theory.

(4) For the Maxwell-Einstein truncation of this theory, the monopole charge equals unity. For this theory N=2 supersymmetry breaks down to N=1 [40]. (Compare this with N=2 supergravities in d=4, which have been shown not to break to N=1 [43]).

Preonic SKK

Following Cremmer and Julia[44], one may compactify d=ll, N=l on $(AdS)^4 \times (S^1)^7$. This theory exhibits chiral SU(8) composite gauge symmetry. The SU(8) chiral symmetry led to the original preonic model of Ellis, Gaillard, Maiani and Zumino [45].

Although Witten made the seminal remark that dim G/H = 7, for $G/H = \frac{SU(3) \times SU(2) \times U(1)}{SU(2) \times U(1) \times U(1)}$ is that $SU(3) \times SU(2) \times U(1)$ may arise naturally for $d = \frac{4}{7} = 11$, d'Auria, Castellani and Fré and RSS have confirmed that quarks

^{*)} Another gravitationally anomaly-free 16-parameter subgroup is $SU(4) \times U(1)$ which may be relevant for preonic models, where the 56 (Majorana-Weyl of E_7) goes to 1 + 6 + 6' + 15 Weyl.

and leptons quantum numbers cannot be described within the compactification AdS x G/H of d=ll SKK. This is additional to the difficulty with chirality. Thus d=ll, SKK can only be used for preons.

The recent compactification of d=ll, N=l on $(AdS)^{4} \times S^{7}$ [6,46] gives rise to a gauged (vector-like) SO(8) symmetry (N=8) in 4 dimensions; however

the fermions can still be classed in terms of a global, chiral SU(8). Recently, Duff, Koh and Nilsson [47] have considered the squashed 7-sphere compactification which has SO(5) x SO(3) (N=0) symmetry [48]. They believe that SU(8) chiral now breaks to SU(5) x SU(3) x U(1). This leads them to consider a new preonic model, where it is shown that 4 families of $5^* + 10$ (bound) massless fermions belonging to SU(5) may be motivated.

VII. CONCLUDING REMARK

From this variety of attempts, the optimist may conclude that with sauged Super-Kaluza-Klein we may be at a stage when an acceptable electro-nuclear stavity model may emerge in not too distant a future. The pessimist will of course point out that we are departing from the unadulterated KK ethic, if quarks and leptons are allowed in as supplementary matter, however restricted. The lure of KK, (for phenomenologists living in four dimensions), at present, is aesthetic but this may change not too distantly.

Appendix I

NOTATION

Notation (A) d space-time dimensions (-+++,+++,..).

(Non)-Abelian gauge symmetries G emerge from spontaneous compactification $M^4 \ge B^{d-4}$; M^4 is 4-space-time manifold (labels \ge_a , a = 0,1,2,3) and B^{d-4} = coset manifold G/H (labels \ge_μ = 1,2,3,... d-4 = dim. G/H = dim. G - dim. H

(B) <u>Spontaneously compactified background (vacuum) metric;</u>

 M^4 = Minkowski or AdS (rather than de Sitter) guarantees that energy E > 0 and supertheories can be formulated; $C_2 > 0$ guarantees compactness of B^{d-4} , i.e. discrete spectrum and a compact gauge group G (see Ref.[49]).

(C) Spectrum

Harmonically expand all fields on G'H; $\phi = \langle \phi \rangle + \phi^{\text{quantum}}$ [50], $\phi(\mathbf{x},\mathbf{y}) = \sum_{n=1}^{\infty} \phi_n(\mathbf{x}) Y_n(\mathbf{y}); \phi_n(\mathbf{x})$ are the physical fields in 4-dimension and $M^2 Y_n = m^2_n Y_n$ (M² is a differential operator on G/H). m_n 's are the masses in the KK <u>spectrum</u> (including zero masses) in d=4. Effective Lagrangian in d=4 is obtained by integrating over y.

(D) Zero mass Yang-Mills fields corresponding to G have a coupling $\alpha \approx G/a^2$, G = Newtonian constant. (The precise proportionality depends on -ixing).

REFERENCES. *

- [1] P. Candelas and S. Weinberg, Nucl. Phys. <u>B237</u>, 397 (1984).
- [2]a M.H. Sarmadi, ICTP, Trieste, preprint IC/84/3 (1984); b S. Randjbar-Daemi and M.H. Sarmadi, to be published.
- [3] A. Chodos, Yale University, preprint YTP 84-06 (1984).
- [4] Z. Horvath, L. Palla, E. Cremmer and J. Scherk, Nucl. Phys. <u>B127</u>, 57 (1977).
- [5] M.J. Duff, B.E.W. Nilsson. C.N. Pope and N.P. Warner, Imperial College, preprint, TP/83-84/56 (1984).
- [6] P.G.O. Freund and M.A. Rubin, Phys. Lett. <u>97B</u>, 223 (1980).
- [7] C. Omero and R. Percacci, Nucl. Phys. B165, 351 (1980).
- [8] M. Gell-Mann and B. Zweibach, Phys. Lett. <u>141B</u>, 333 (1984).
- [9] W. Marciano, Brookhaven National Lab., preprint BNL-33980 (1984).
- [10] S. Randjbar-Daemi, Abdus Salam and J. Strathdee, Phys. Lett. <u>B135</u>, 388 (1984).
- [11] D. Bailin, A. Love and C.E. Vayonakis, Sussex University, preprint (1984) (to appear in Phys. Lett., 1984).
- [12] P. Ramond, in Proceedings of John Hopkins Workshop on Current Problems on High Energy Particle Theory, Florence, Italy (1982).
- M. Gleiser, S. Rajpoot and J.G. Taylor, King's College, preprint (1984);
 Y. Okada, University of Tokyo, preprint UT-429 (1984);
 R. Bergamini and R. Capovilla, Bologna, internal report (1984).
- [14] E. Alvarez and B. Belén Gavela, Phys. Rev. Lett. <u>51</u>, 931 (1983);
 Q. Shafi and C. Wetterich, Phys. Lett. <u>129B</u>, 387 (1983);
 D. Sahdev, Phys. Lett. <u>137B</u>, 155 (1984).
 S.M. Barr and L.S. Brown, Univ. Washington, Seattle, preprint 40048-01 P4 (1984);
 M. Yoshimura, Ibaraki, preprint KEK-TH 89 (1984);
 T. Koikawa and M. Yoshimura, Ibaraki, preprint KEK-TH 91 Revised (1984);
 R.B. Abbott, S.M. Barr and S.D. Ellis, Univ. Washington, Seattle, preprint 40048-03 P4 (1984).
- [15] S.A. Eludman, Nature <u>308</u>, 319 (1984);
 A.H. Guth and M. Sher, Nature <u>302</u>, 505 (1983).
- [16] E.W. Kolb and R. Slansky, Fermi Lab, preprint 83/88/AT (1983).
- [17] A. Chodos and S. Detweiler, Phys. Rev. <u>D21</u>, 2167 (1980).
- [18] R. Sorkin, Phys. Rev. Lett. <u>51</u>, 87 (1983);
 D.J. Gross and M.J. Perry, Nucl. Phys. <u>B226</u>, 29 (1983);
 P. Follard, J. Phys. <u>A16</u>, 565 (1983);
 D. Nelson, Nucl. Phys. <u>238B</u>, 638 (1984);
 Z.F. Ezawa and A. Iwasaki, Imperial College, preprint TP 33-84/8 (1984);
 F.A. Bais, Lectures presented at the Cargese (1983) (to be published).
- [19] L. Alvarez-Gaumé and E. Witten, Nucl. Phys. <u>B234</u>, 269 (1984).
- [20] L.N. Chang and H.T. Nieh, Phys. Rev. Lett. <u>53</u>, 21 (1984).
- [21] W.A. Bardeen and B. Zumino, Univ. of California, LBL preprint 17639 (1984).

^{*)} This list is not exhaustive; only references relevant to material covered in these notes are included.

- [22] L. Bonora and A. Pasti, Phys. Lett. <u>132</u>, 75 (1984).
- [23] P.H. Frampton and T.W. Kephart, Univ. of North Carolina, preprint IFP-193-UNC (1983).
- [24]a L. Caneschi, G. Farrar and A. Schwimmer, Phys. Lett. <u>133B</u>, 386 (1984);
 b R. Delbourgo and P.D. Jarvis, Phys. Lett. <u>B136</u>, 43 (1984).
- [25] S. Randjbar-Daemi and R. Percacci, Phys. Lett. 117B, 41 (1982).
- [26] S. Randjbar-Daemi, Abdus Salam and J. Strathdee, Phys. Lett. <u>124B</u>, 345 (1983); see Erratum.
- [27] A.N. Schellenkens, Stony Brook, preprint ITP-SB-84-29 (1984).
- [28] L. Palla, Tokyo Conf. Report, p.629 (1978).
- [29] S. Randjbar-Daemi, Abdus Salam and J. Strathdee, Nucl. Phys. <u>B214</u>, 491 (1983).
- [30] S. Randjbar-Daemi, Abdus Salam.and J. Strathdee, ICTP, Trieste, preprint IC/84/62 (unpublished) (1984).
- [31] G. Wetterich, University of Bern, preprint BUTP-84-6 (1984). SO(N=12) is considered to construct SO(10) x (SU(2) x U(1)) family model.
- [32] P. Forgaćs, Z. Horvath and L. Palla, Hung. Acad. Sci., Budapest, preprint (1984).
- [33]a S. Randjbar-Daemi, Abdus Salam and J. Strathdee, Phys. Lett. <u>132B</u>, 56 (1983);
 b S. Randjbar-Daemi, Abdus Salam and J. Strathdee, Nucl. Phys. <u>B242</u>, 447 (1984).
- [34]a P.H. Frampton and K. Yamamoto, Univ. of North Carolina, preprint IFT-222-UNC (1984);
 - b P.H. Frampton, P.J. Moxhay and K. Yamamoto, Univ. of North Carolina, preprint IFT-229-UNC (1984).
- [35] E. Witten, Princeton University, preprint (1983).
- [36] S. Randjbar-Daemi, Abdus Salam and J. Strathdee, Phys. Lett. <u>124B</u>, 349 (1983;
 C. Chapline and G. Gibbons, Univ. of California, preprint UCRL-90924 (1984).
- [37] D. Olive and P.C. West, Nucl. Phys. <u>B127</u>, 248 (1983).
- [38] Abdus Salam and E. Sezgin, to be published.
- [39] H. Nishino and E. Sezgin, Phys. Lett. <u>144B</u>, 187 (1984).
- [40] Abdus Salam, and E. Sezgin, ICTP, Trieste, preprint.IC/84/57 (1984) (to appear Phys. Lett. B) (1984).
- [41] I.G. Koh and H. Nishino, ICTP, Trieste, preprint IC/84/129 (1984).
- [42] J.Bagger and E. Witten, Princeton Univ., preprint (1983).
- [43] S. Cecotti, L. Girardello and M. Parrati, Milan Univ., preprint (1984).
- [44] E. Cremmer and B. Julia, Nucl. Phys. <u>B159</u>, 141 (1979).
- [45] J. Ellis, M. Gaillard, L. Maiani and B. Zumino in <u>Unification of the</u> <u>Fundamental Particle Interactions</u>, Eds. S. Ferrara, J. Ellis and P. van Nieuwenhuizen (Plenum Press, New York, 1980) p.727.
- [46] M.J. Duff and C.N. Pope, in <u>Supersymmetry and Supergravity'82</u>,
 Eds. S. Ferrara, J.G. Taylor and P. van Nieuwenhuizen (World Scientific Publ. Comp., Singapore, 1983).
- [47] M.J. Duff, I.G. Koh and B.E.W. Nilsson, Imperial Coll., preprint TP/83-84/50 (1984
- [48] M.A. Awada, M.J. Duff and C.N. Pope, Phys. Rev. Lett. 50, 294 (1983).
- [49] M.J. Duff, Imperial College, preprint TP/83-84/45 (1984).
- [50] Abdus Salam and J. Strathdee, Ann. Phys. 141,316 (1982).

- [51] E. Cremmer, B. Julia and J. Scherk, Phys. Lett. <u>76B</u>, 409 (1978);
 M.J. Duff, B.E.W. Nilsson and C.N. Pope, to appear in Physics Reports and references therein;
 P. van Nieuwenhuizen, Les Houches Lectures (1983), and references therein;
 L. Castellani, R. D'Auria and P. Fre^e, Nucl. Phys. <u>B239</u>, 610 (1984).
- [52] M. Huq and M.A. Namazie, ICTP, Trieste, preprint IC/83/210 (1983);
 I.C.G. Campbell and P.C. West, King's College, preprint (1984);
 B.E.W. Milsson and C.N. Pope, Imperial College, preprint TP/83-84/41 (1984);
 F. Giani and M. Pernici, Stony Brook, preprint ITP-SB-84-13 (1983).
- [53] M.E. Green and J.H. Schwarz, Phys. Lett. <u>109B</u>, 444 (1982);
 J.H. Schwarz and P.C. West, Phys. Lett. <u>126B</u>, 301 (1983);
 P.S. Howe and P.C. West, King's College, preprint (1983).
- [54] G.F. Chapline and N.S. Manton, Phys. Lett. <u>120B</u>, 105 (1983);
 E. Bergshoeff, M. de Roo, B. de Wit and P. van Nieuwenhuizen, Nucl. Phys. <u>B195</u>, 97 (1982).
- [55] S.J. Gates, Jr., H. Nishino and E. Sezgin, ICTP, Trieste, preprint IC/84/105 (1984).
- [56] Abdus Salam and E. Sezgin, Phys. Lett. <u>118B</u>, 359 (1982).
- [57] M. Pernici, K. Pilch and P. van Nieuwenhuizen, Phys. Lett. <u>143B</u>, 103 (1984);
 P.K. Townsend and P. van Nieuwenhuizen, Phys. Lett. <u>125B</u>, 41 (1983);
 M. Pernici, K. Pilch, P. van Nieuwenhuizen and N.P. Warner, Stony Brook,
 preprint ITP-SB-84-41 (1984);
 - A. Salam and E. Sezgin, Phys. Lett. <u>126B</u>, 295 (1983);
 M. Pernici and E. Sezgin, ICTP, Trieste, preprint IC/84/117 (1984).
- [58] Y. Tanii, Tokyo, preprint TIT/HEP-79 (1984).
- [59] F. Giani, M. Pernici and P. van Nieuwenhuizen, Stony Brook, preprint ITP-SB-84-35 (1984).
- [60] P.K. Townsend, Univ. of Texas, preprint UTTG-11-83 (1983).
- [61] N. Marcus and J.H. Schwarz, Phys. Lett. <u>115B</u>, 111 (1982);
 R. D'Auria, P. Fré and T. Regge, Phys. Lett. 128B, 44 (1983).

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G _{YM}	Stability of embedding of U(l) into G _{YM}	Low Energy Sym, of ^L effective	# of chiral fermions	References
נו)	Stable	SU(2)xU(1)	n =2q+1 q rep. of SU(2)	[28,29]
SO(N) N > 2	Stable only if under $SO(N) \rightarrow SO(N-2)xO(2)$ we have $N \rightarrow (N-2)_0^{+1}_{1/2}^{+1}_{-1/2}$	SU(2)xU(1)x xSO(N-2)		[27,30,31]
$su(n)/Z_{N}$ $n > 2$ e.g. $\frac{su(3)}{Z_{3}}$	Stable A = 1/2dφ(cos0¥1) x diag.(1/3,1/3,-2/3)			[32,26]
e.g. SU(N), Sp(N),Spin(N) or excep- tional groups	perturbatively unstable			[27,26]

 $G/H = S^2 = \frac{SU(2)}{U(1)}$ < A > = L⁻¹dL|_H Monopole compactification **d** = 6

Table I : Monopole compactifications of d = 6 Kaluza-Klein theories.

TABLE II

d = 8	Instanton compactification	$G/H = S^4$	$= \frac{30(9)}{\mathrm{SU}(2) \times \mathrm{SU}(2)}$	
G _{YM}	Embedding of instanton (instanton number k=1)	Low energy symmetry	# chiral fermions	References
SU(2)	Stable	SO(5) (note SU _{YM} (2) is broken)	(2/3)q(q+1)(2q+1)	[3 3a,33b]
All groups	Stable			[30,34b]
SO(N)	4x4 top corner of the NxN matrix for SO(N)	SO(5)xSU(2)x x SO(N-4)	Starting with chiral rep. of SO(1,7)xSO(N), massless fermion rep. is (1,1,2N/(?-1) of SO(5)xSU(2)xSO(N- ^{1,}) after compactification	[30]
50(N)	3x3 top corner	SO(5)xSO(N-3)	massless rep. after compactification is $(1,2^{[N/2]})$	[30]

 $G/H = S^{4} = \frac{SO(5)}{SO(5)}$ Instanton compactification

Table II : Instanton induced compactification of d = 8 Kaluza-Klein theories. Anomaly free representations of SO(14) will give a realistic one-family SO(10) electro-nuclear-gravity [30] or three families, e.g. take anomaly free SU(11) representation: $[4]_{L} + [3]_{R} + [2]_{R} + [1]_{R}$ (or SU(9) representation = $[3]_{L} + 9[1]_{R}$) where [k] is an antisymmetric representation of order k [34a]. In the case of $SO(5) \times SO(N-3)$ low energy symmetry, there exists a massless scalar (5,N-3) which may be used to break the symmetries using the Coleman-Weinberg mechanism.

Embed. < A > = spin-connection	G/H	<pre># chiral families</pre>	Remarks
16 x 16 matrix	s ⁶	2 families	<pre># family = Euler characteristic of G/H (Witten)</pre>
	$s^2 \times s^4$	4 families	
0	$s^2 \times s^2 \times s^2$	8 families	
0(6)	CP(3)	4 families	No anti-families
	$s^3 \times s^3$	O families	

Table III: d = 10 The Witten model [35] $G_{\rm YM} = O(16)$ with fermions in the anomaly-free representation: $(128_{+L}, 128_{-R})$ where (L,R) specify tangent space O(1,q) chirality and +,- refer to Weyl decomposition of O(16) representations. This would be a fine model with no massless antifamilies of SO(10). RSS show, however, that this model contains tachyons and is unstable [30].

S/R	Fermionic content (R rep.)
$E_{7}/SO(12) \times Sp(1)$ $E_{8}/E_{7} \times Sp(1)$ $E_{6}/SU(6) \times Sp(1)$ $F_{4}/Sp(3) \times Sp(1)$ $G_{2}/Sp(1) \times Sp(3)$ $SO(n,4)/SO(n) \times SO(3) \times Sp(1)$ $Sp(n,1)/Sp(n) \times Sp(1)$ $Sp(1) \times Sp(1)$	$\psi^{a}: (32,1)$ (56,1) (20,1) (14,1) (4,1) (1,2,1) (2n,1) (2n,1)
$SU(n,2)/SU(n) \times Sp(1) \times U(1)$	(n+n,⊥,q)

TABLE IV

Table IV : Quaternionic Kahler manifolds.

TABLE	V
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Dim.	N	Degrees of freedom	Gauging	Gauge group	Compactification	Anomaly free	References
d=11	N=1	128	No	-	AdS x $(S^7, J^7, M^{pqr},)$	Yes	[51]
	N=2	128	No	-	$Ads(CP^3, CP^2 \times s^2, \dots)$	Yes	[52]
d=10 -	*N=2	128	No	-	M ⁸ x Tear Drop, (AdS) ₅ x K ³	Yes	[53]
	*N=1+ matter	64	No	-	?	No	[54]
4-0	N=2	128	?	?	?		
d=9 -	N=1+ matter	56	No	-	?		[55]
	N=2	128	Yes	SU(2)	Ads x (s^4, CP^2, \dots)	Yes	[38]
d=8 -	N=1+ matter	48	No	-	?	Yes	
N=4 128 ? d=7 N=4 128 Ye N=2+ matter 40 Ye	N=1	128	?	?	?	Yes	[56]
	Yes	SO(p,q) p+q=5	Ads x (s ³ ,H ³)		[57]		
	N=2+ matter	40	Yes	SU(2)	AdS x H ³		[57]
	N=8	128	?	?	?	Yes	[58]
 d=6 	*n=8	128	?	?	?	No	
	N=4+ matter	32	Yes	SU(2)	?	Yes	[59]
	*N=4+ matter	32	No	-	.?	Yes	[60]
	*N=2+ matter	16	Yes	SU(2) (or U(1))	M ⁴ x s ²	No	[39,40,41,61]

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Table V : Status of SKK theories. Chiral theories are indicated by *. $M^{\underline{l}_{4}}$ denotes $\underline{l}_{4}\text{-dimensional Minkowski space.}$ In the fourth column gauging refers to vector fields of the supergravity multiplet. Whenever matter Yang-Mills multiplet exists (see first column) it can be coupled to the supergravity multiplet non-minimally (i.e. Pauli type coupling).