

P5b

Particle Spectroscopy, Theoretical

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§ 1. Introduction

There were only five particles on the list of the elementary particles, when Professor Yukawa, the President of this Conference, invented the pions forty four years ago.¹

At that time the proton, neutron and electron were considered to be the basic constituents of matter, and nuclear forces were proposed to be mediated by pions.

Since then, an enormous number of particles have been discovered. For example, there were an exciting discovery of the *Y* particle last summer and confirmation of *Y'* we have just heard at this Conference.

Now the colored quarks with flavors are considered to be the basic constituents of hadrons, and we have quantum chromodynamics (QCD) as a promising candidate of the dynamics of the strong interaction.

Today I will try to report on the progress of particle spectroscopy from this point of view.

I will speak about
charmonium,

R,

spectroscopy of old hadrons and QCD,
charmed hadrons,

baryonium,

and

dibaryons.

§ 2. Charmonium

At first let us discuss charmonium. We show the levels and branching ratios of the known charmonium in Fig. 2. I.^{2,13}

Qualitatively the level structure of the *Jj(p)* family of new particles can be explained as charmonium, *i.e.*, as a charmed quark-antiquark (*cc*) system bound nonrelativistically by a potential suggested by the idea of QCD. However, there are still two serious problems in this model, the hyperfine splittings of 1*S* and 2*S* states and the magnitudes of the

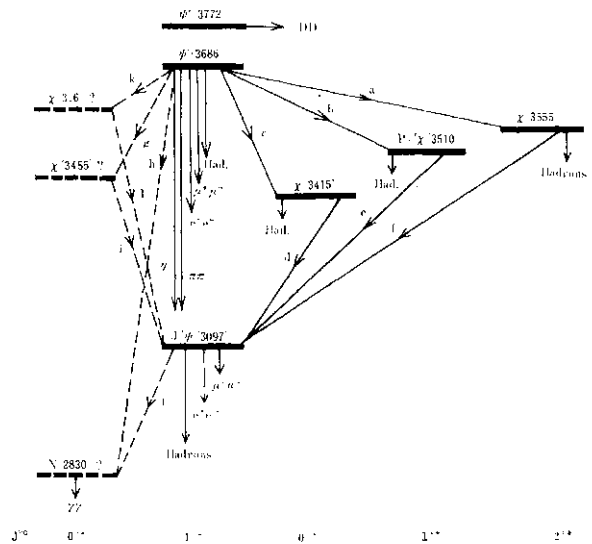


Fig. 2. 1. Charmonium.

Branching ratios of *γ*-decays; *a* = 7 ± 2%, *b* = 7 ± 2%, *c* = 7 ± 2%, *d* = 16 ± 3%, *e* = 23.4 ± 0.8%, *f* = 3.3 ± 1.0%, *g* < 2.5%, *h* < 1.0%, *ig* ≈ 0.5%, *j* < 1.7%, *kl* = 0.28 ± 0.12%. Data are taken from refs. 2, 3 and particle data group, Phys. Lett. 75B (1978) i.

M1 transition rates if JST(2.83) and ψ(3.455) are to be identified with the 1*S*₀ and 2*S*₀ state.

The contribution of the spin-spin interaction,⁴ (327ca,19m²)*s*₁*S*₂δ(*r*), arising from the exchange of a single color-gluon to the hyperfine splitting is given by

$$\Delta M = \frac{32\pi\alpha_s}{9m_c^2} |\phi(0)|^2 \approx \begin{cases} 36 \text{ MeV for } 1S \\ 15 \text{ MeV for } 2S, \end{cases} \quad (2.1)$$

for $\alpha_s \approx 0.19$ and $a_s = 0.19$. Here, $a_s(m) = 0.19$ was obtained by applying the formula⁵ $T_{ij}(\text{hadrons}) \ll R(V \rightarrow ggg) = (160/81)(7r^2 - 9)(a^3/M^2)|\phi(0)|^2$ to $f(1/1 \text{ hadrons})$. Here, we used the magnitudes of $|\phi(0)|^2$ determined from⁶ $\Gamma(F \rightarrow p^+p^-) = 16a^2 e^2 |\phi(0)|^2 / M^2$. The predicted mass differences (2.1) should be compared with the experimental values of 270 and 230 MeV, respectively.

In the nonrelativistic approximation, the decay width of the M1 transition $Jjcp \rightarrow XA-j$ is predicted to be 29 keV, while experimentally it is < 1 keV.

Let us discuss these problems.

The potential suggested by the idea of QCD consists of spin independent part and spin dependent part,

$$U(r) + U_{\text{spin}}(r). \tag{2.2}$$

Traditionally spin independent potential $U(r)$ is a sum of a phenomenological long-range confining potential assumed to vary linearly with distance and a short-range Coulomb type potential arising from the exchange of a single color-gluon between the quarks,⁷

$$U(r) = ar - \frac{4}{3} \frac{\alpha_s}{r}. \tag{2.3}$$

Since the confining potential is considered to arise from multiple-gluon-exchanges, it consists of Lorentz-vector part $j^{\mu} \otimes 7 \rightarrow \dots$ and scalar part $1(x)$ (and pseudoscalar part $y \wedge j$ etc.⁸)

This spin independent potential $U(r)$ yields the following generalized Breit-Fermi potential for fine and hyperfine splittings,⁹⁻¹³

$$U_{\text{spin}} = \frac{1}{3m_c^2} \left(\frac{d^2 V}{dr^2} - \frac{1}{r} \frac{dV}{dr} \right) [s_1 \cdot s_2 - 3(s_1 \cdot \hat{r})(s_2 \cdot \hat{r})] + \frac{2}{3m_c^2} s_1 \cdot s_2 \nabla^2 V(r) + \frac{1}{2m_c^2 r} \left(3 \frac{dV}{dr} - \frac{dS}{dr} \right) (\mathbf{r} \times \mathbf{p}) \cdot (s_1 + s_2), \tag{2.4}$$

where V and S denote Lorentz-vector and scalar part¹⁴ of $U(r)$,

$$\begin{aligned} U(r) &= V(r) + S(r), \\ V(r) &= -\frac{4}{3} \frac{\alpha_s}{r} + far, \\ S(r) &= (1-f)ar. \end{aligned} \tag{2.5}$$

The contribution of pseudoscalar part, ⁷⁻⁵⁽⁸⁾⁷⁻⁵, due to multiple-gluon-exchanges to spin dependent potential is neglected for simplicity.

In order to explain the observed ³P_J splittings the fraction of Lorentz-vector vertices $V=1$. For $f=1$, $|A^{\wedge} M \zeta P J - M \zeta P i| / [M m - i M \zeta P o J \wedge O \hat{a}]$ while the experimental value of this ratio is about 0.42.

Quantitatively it is impossible to reproduce the hyperfine structure of the charmonium by this potential. The splitting of the $1S$ states, $M(1^3S_1) - M(1^1S_0)$, is found to be less than about 100 MeV, which should be compared with the experimental value, $M(J < p) - M(X) = 270$ MeV.

One proposal to avoid this difficulty is to

introduce an anomalous color "magnetic" term¹² K to the vector part of the linear confining potential far .¹⁵⁻¹⁸ Then, the term far in the tensor and spin-spin interactions in (2.4) are multiplied by a factor $(1+r)^2$ and that in the LS interaction is multiplied by a factor $(1+A)$. This hypothesis provides an extra parameter and can reproduce all of $1S$, $2S$ and ³P_J splittings simultaneously¹⁹ for $f \approx 4 \sim 5$, $f \ll 0.1$ and $a \wedge 0.45$.

According to another proposal, instantons are responsible to the splitting of $J < p$ and rj . Unfortunately there is no quantitatively reliable calculation of the contributions of instantons to the splitting. According to Wilczek and Zee,²⁰

$$M(J < p) - M(\chi) \sim 37 r^4 v^4 / m^2 c \sim 450 \text{ MeV}, \tag{2.6}$$

where u is the usual renormalization scale and taken to be about 200 MeV. However, the numerical result is very sensitive to the cutoff in the size of the instantons.²¹

Next let us discuss electromagnetic transitions of the charmonium.

The E1 transition rates have been reproduced fairly well in the charmonium model.^{22,23}

In the nonrelativistic quark model the M1 transition rates are expressed as^{22,23}

$$\begin{aligned} \Gamma(M1) &= \frac{4}{3\pi} (2J_f + 1) k^3 \mu_c^2 \\ &\times | \langle f | -1 + \frac{k^2 r^2}{24} | i \rangle |^2. \end{aligned} \tag{2.7}$$

Therefore,

$$\Gamma_{\text{allowed}}(M1) = \frac{4}{3\pi} (2J_f + 1) k^3 \mu_c^2, \tag{2.8}$$

and

$$\Gamma_{\text{forbidden}}(M1) = \frac{1}{72\pi} \frac{k^7}{m_c^2 \omega^2} (2J_f + 1) \mu_c^3, \tag{2.9}$$

where $ix_c = e \cdot e / 2m_c c$ and for simplicity we have used the wave functions of the harmonic oscillator potential in evaluating $\langle 1S | r^2 | 2S \rangle$.

If we identify X(2.83) with $y_c(1^3S_1)$ and (3.45) with $rj_c(2^1S_0)$, we obtain the following predictions from (2.8) and (2.9),

$$\Gamma(J/\psi \rightarrow X\gamma) = 29 \text{ keV} \rightarrow Br(J/\psi \rightarrow X\gamma) = 40\%, \tag{2.10a}$$

$$\Gamma(\psi' \rightarrow X\gamma) = 8.5 \text{ keV} \rightarrow Br(\psi' \rightarrow X\gamma) = 4\%, \tag{2.10b}$$

$$\Gamma(\chi(3.45) \rightarrow J/\psi\gamma) = 0.13 \text{ keV}, \tag{2.10c}$$

$$\Gamma(\psi' \rightarrow \chi(3.45)\gamma) = 21 \text{ keV} \rightarrow Br(\psi' \rightarrow \chi(3.45)\gamma) = 9\%, \quad (2.10d)$$

where $m_{\psi'} = 1650 \text{ MeV}$ and $m_{\chi} = 330 \text{ MeV}$ determined from $M(\langle p' \rangle) - M(J/\psi)$ and $e^+e^- \rightarrow \psi' \rightarrow \chi(3.45)\gamma$ are used. (See, Fig. 2.2.) All of these predictions are sources of troubles. Experimental results, $Br(J/\psi \rightarrow \chi(3.45)\gamma) < 0.5\%$, $Br(\psi' \rightarrow \chi(3.45)\gamma) < 2.5\%$, are not compatible with the above theoretical values, and (2.10c) and the experimental results²⁴ $Br(\psi' \rightarrow \chi(3.45)\gamma) > 20\%$ predict $P(\chi(3.45)) < 0.1 \text{ keV}$, which seems too small.

However, forbidden transition rates are not reliable since the matrix elements depend sensitively on the choice of the confining potential. For example, if we include spin-spin interaction in the unperturbed Hamiltonian, $\langle 1^1S^0 \rangle$ and $\langle 1^3S_1 \rangle$ are no longer zero and the forbidden MI transition rates increase considerably.²³ There are also relativistic correction terms²⁵ $\langle \frac{1}{2} \frac{p^2}{m^2} \rangle + \langle \frac{f(S(r)/m_c)j_c(kr/2)|i\rangle}{m_c} \rangle$ to be added to the radial matrix element $\langle \frac{1}{r} | -1 + (\frac{1}{2} \frac{V^2}{24}) | \rangle$.

One proposed solution to the MI troubles is as follows. $X(2.83)$ and $\chi(3.45)$ are not r_{j_c} and r_{j_c} . Instead there are real r_{j_c} and r_{j_c} with $100 \text{ MeV} > M(\langle \chi \rangle) - M(O^?) > 0$ and $50 \text{ MeV} > M(O) - \text{Aff} O^? O$. Then, what is $X(2.83)$ and $\chi(3.45)$? Lipkin has suggested²⁶ that $X(2.83)$ and $\chi(3.45)$ are $ccqq$ states ($q=u$ and/or d) and that

there are two 0^+ mesons, one with $J=0$ and another with $J=1$. He has also suggested that $\chi(3.45)$ is a cress state with $J=0$. In order to test Lipkin's conjecture one should search for the transition $\langle p' \rangle + Xp$ since its observation indicates that X is not a cc state.

Now let me mention that the assignment of $X(2.83)$ to Y_{J_c} has another problem; If we use the formula, $F(T_{J_c} \rightarrow \gamma\gamma) = 48 \pi^2 V_0 \langle p(0) | 7 M(r)_{J_c} \text{ and } F(T_{J_c} \text{ hadrons}) \gg F(r_{j_c} \rightarrow gg) = (32/3) a^2 |0(O)|^2 / M(O)^2$, we find

$$Br(\gamma_c \rightarrow \gamma\gamma) \approx 10^{-3}, \quad (2.11)$$

while we obtain

$$Br(X \rightarrow \gamma\gamma) \geq 0.008 \quad (2.12)$$

from experimental results $Br(J/\psi \rightarrow \chi(3.45)\gamma) Br(X \rightarrow \gamma\gamma) = \{A \pm 0A\} \times 10^{-4}$ and $Br(J/\psi \rightarrow \chi(3.45)\gamma) < 0.7\%$

The large branching ratio $Br(X \rightarrow \gamma\gamma) > 0.00\%$ indicates that hadronic decays of X are forbidden, for example, by flavor selection rules.

Finally let us discuss the candidate of a new charmonium level at 3.6 GeV observed in the $S^1 + Y_{J_c} J/\psi \rightarrow p$ decay and reported at this Conference.^{27,28} If we identify this resonance with r_{j_c} , the allowed MI transition rate is predicted to be

$$\Gamma(\psi' \rightarrow \chi(3.6)\gamma) = 1.1 \text{ keV} \rightarrow Br(\psi' \rightarrow \chi(3.6)\gamma) = 0.5\%, \quad (2.13)$$

and the forbidden MI transition rate is predicted to be

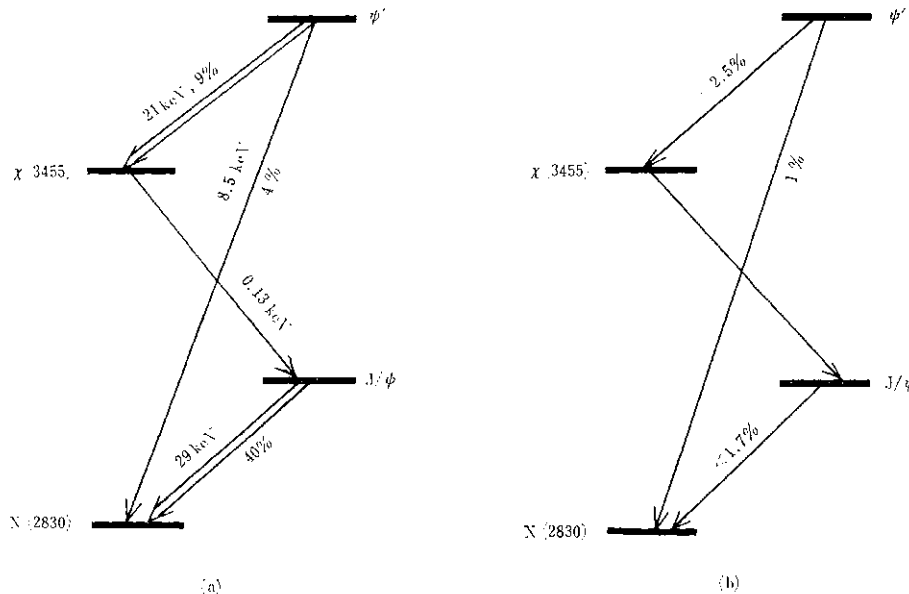


Fig. 2.2. MI transitions, (a) Theory; (b) Experiment.

$$\Gamma(\chi(3.6) \rightarrow J/\psi\gamma) = 10 \text{ keV}. \quad (2.14)$$

Since experimentally³

$$\begin{aligned} Br(\psi' \rightarrow \chi(3.6)\gamma) Br(\chi(3.6) \rightarrow J/\psi\gamma) \\ = (2.8 \pm 1.2) \times 10^{-3}, \end{aligned} \quad (2.15)$$

the branching ratio of the forbidden M1 transition is predicted to be

$$Br(\chi(3.6) \rightarrow J/\psi\gamma) \approx 60\%, \quad (2.16)$$

which is too large to be acceptable, it seems that the experimental result (2.15) is possible only if both radiative transitions are E1 transitions. This means that the spin-parity of the new resonance is 0^+ , 1^+ or 2^+ .

§3. \mathbf{r}

Y was observed last summer as a strong enhancement at 9.5 GeV in the mass spectrum of dimuons produced in 400 GeV proton-nucleus collisions,²⁹

$$p + (\text{Cu, Pt}) \rightarrow \mu^+ + \mu^- + \text{anything},$$

at Fermilab. Later they found two peaks whose widths are consistent with their resolution and evidence for the possible existence of a third peak.³⁰

Three months ago Y was confirmed by using the PLUTO and DASP detectors at DORIS in the reaction,³¹

$$e^+ + e^- \rightarrow \text{hadrons}.$$

According to their latest results³¹

$$\begin{aligned} M(Y) &= 9.46 \pm 0.01 \text{ GeV}, \\ \Gamma_s(Y) &> 25 \text{ keV (95\% CL)} \\ &\quad (\text{best value } 50 \text{ keV}), \\ \Gamma_{ee}(Y) &= 1.3 \pm 0.2 \text{ keV}. \end{aligned}$$

At this Conference the confirmation of Y' at DORIS has been reported. According to their results,³

$$\begin{aligned} M(Y') - M(Y) &\approx 556 \text{ MeV}, \\ \Gamma_{ee}(Y') / \Gamma_{ee}(Y) &\approx 3. \end{aligned}$$

It is quite natural to regard the T-particle as a bound state of a new heavy quark and its

antiparticle. While the existence of the charmed quark was predicted based on the lepton-hadron symmetry³² and the absence of the strangeness changing weak neutral current,³³ a six-quark model was proposed by Kobayashi and Maskawa³⁴ in 1973 in order to explain CP nonconservation in the gauge model.³⁵ Properties of the six quarks, u, d, s, c, t and b, are summarized in Table I.

In Table I T and B are new quantum numbers conserved in both strong and electromagnetic interactions. The charges of hadrons are expressed as

$$Q = I_3 + \frac{1}{2}(B + S + C + T + B).$$

Let us determine the charge of the new heavy quark e_0 from the leptonic decay width of Y by making use of the nonrelativistic relation,⁶

$$\Gamma(V \rightarrow e^+e^-) = 16\pi\alpha^2 e_q^2 |\phi_q(0)|^2 / M_v^2, \quad (3.1)$$

where $|\phi_q(0)|$ is the magnitude of the qq wavefunction of the vector-meson V at the origin.

From the leptonic decay widths of $p, a, \langle f \rangle$ and J/ψ Jackson derived an empirical formula,²²

$$|\phi_q(0)|^2 \propto M_v^{1.89 \pm 0.15}. \quad (3.2)$$

Therefore, $r(V \rightarrow e^+e^-) / e_0^2$ should be nearly independent on the mass of the vector-meson³⁶ M_v , and we find

$$e_0^2 \approx \frac{1}{9} \text{ but } \neq \frac{4}{9} \quad (3.3)$$

as we can clearly see in Fig. 3. 1, in which $r(V \rightarrow e^+e^-) / e_0^2$ vs M is plotted.

The conclusion (3.3) is also reached by comparing the lower bounds

$$\Gamma(Y \rightarrow e^+e^-) / e_0^2 > 2.6 \text{ keV}$$

and

$$r(X \rightarrow e^+e^-) / e_0^2 > |A| \text{ keV}, \quad (3.4)$$

with the experimental results from DORIS. The lower bounds (3.4) were derived by Rosner, Quigg and Thacker³⁷ for potentials which are

Table I. Properties of six quarks.

Quark	Q	B	I	I_3	S	C	T	B
u	2/3	1/3	1/2	1/2	0	0	0	0
d	-1/3	1/3	1/2	-1/2	0	0	0	0
s	-1/3	1/3	0	0	-1	0	0	0
c	2/3	1/3	0	0	0	1	0	0
t	2/3	1/3	0	0	0	0	1	0
b	-1/3	1/3	0	0	0	0	0	-1

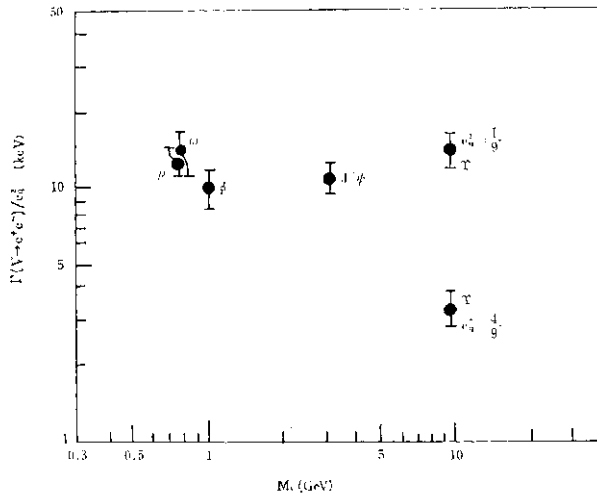


Fig. 3. 1. $\Gamma(Y \rightarrow e^+e^-)/\alpha_s^2$ vs M_q .

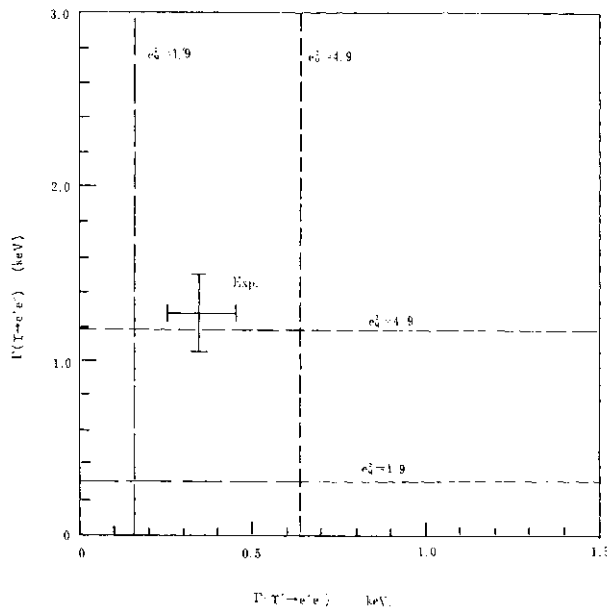


Fig. 3. 2. $\Gamma(Y' \rightarrow e^+e^-)$ vs $\Gamma(Y \rightarrow e^+e^-)$.

Lower bounds on these leptonic decay widths for $\alpha_s^2=4/9$ and $1/9$ are shown (broken lines). The observed value of $\Gamma(T \rightarrow e^+e^-)$ is incompatible with the lower bound if $\alpha_s^2=4/9$. This figure is taken from ref. 37.

concave-downward, $d^2F/dr^2 < 0$. In deriving these lower bounds they have assumed that $m_b/m_c > 2.6$ and made use of the experimental results $\Gamma(J/\psi \rightarrow e^+e^-) = (4.5 \pm 0.6)$ keV and $\Gamma(\psi \rightarrow e^+e^-) = (2A \pm 0.3)$ keV. We find that the experimental value of $\Gamma(\psi \rightarrow e^+e^-)$ is incompatible with the lower bound (3.4) in the case of $A = 4/9$. (See Fig. 3.2.)

Of course, the best way to prove that Y is a bound state of b and \bar{b} is to find an isodoublet of "beautiful" ("bottom") mesons, $B^0 = (b\bar{d})$ and $B^- = (b\bar{u})$.

The dominant decay modes of these mesons

involve charmed mesons,

$$5^0, 2^? \sim \rightarrow a \text{ charmed meson} + \text{wr.}$$

Last year several papers on the bound states of a new heavy quark and its antiparticle were published. For example, before the discovery of Y Eichten and Gottfried³⁸ calculated the energy levels to be expected from the potential model used in charmonium. Their potential

$$U(r) = -\frac{4}{3}\alpha_s(m_c^2)/r + r/a^2 \quad (3.5)$$

($a_s(r) = 0.19$ and $a = 2.22 \text{ GeV}^{-1}$) predicts $M(\psi') - M(\psi) = 420 \text{ MeV}$, which should be compared with the experimental result, 556 MeV.

The difference of the predicted and experimental level spacing $M(Y') - M(Y)$ suggests that the shape of the above potential must be modified, and it has been noticed³⁹ that the apparent equal spacing,

$$M(Y') - M(Y) \approx M(\psi') - M(J/\psi); \quad 556 \text{ MeV}$$

vs 588 MeV, is realized in the nonrelativistic limit if a logarithmic potential⁴⁰

$$U(r) = C \ln(r/r_0), \quad C \approx 0.75 \quad (3.6)$$

is used instead of (3.5).

Though $U(r) = C \ln(r/r_0)$ is unique in giving level spacing independent of the quark mass, the equal spacing, $M(Y') - M(Y) \approx M(\psi') - M(J/\psi)$, is reproduced by the modified Coulomb Potential^{39,41}

$$U(r) = -\frac{4}{3}\alpha_s/r + r/a^2 \quad (3.7)$$

with $\alpha_s = 0.45$ and $a = 2.48 \text{ GeV}^{-1}$. It is interesting to notice that the value a_{QCD} is the value used in order to reproduce the $1S$, $2S$ and $3P_j$ splittings of charmonium.

Now let us consider the magnitude of the quark-gluon fine structure constant, $\alpha_s(q^2)$. In QCD

$$\alpha_s(q^2) \approx [12\pi/(33 - 2F)]/\ln(q^2/\Lambda^2), \quad (3.8)$$

where F is the number of quark flavors. Various experimental data, e.g., scaling violations in deep inelastic reaction indicates⁴² $\Lambda = 0.3 \sim 0.7 \text{ GeV}$. If we use (3.8) with $\Lambda = 0.5 \text{ GeV}$, we find $\alpha_s(m_l) = 0.63$; and if we choose $\Lambda = 0.3 \text{ GeV}$, we find $\alpha_s(m_l) = 0.8$. These results are by a factor of three or two bigger than the value $\alpha_s(m_c) = 0.19$ obtained at time-like $q^2 = m_c^2$.

However, we have to notice that the running

constant $a(q^2)$ evaluated at time-like $q^2=-m_c^2$ and that evaluated at space-like $q^2=m_c^2$ are different in general since q^2 is finite.⁴³

Now let us discuss one-gluon-exchange potential. Because of the q^2 dependence of a_s , which is expressed in (3.8), the $1/r$ behavior of the Coulomb type potential is modulated by an inverse log factor. The asymptotic form of the Fourier transform of $oc(q^2)/q^2$ as $r \rightarrow 0$ is given by⁴⁴

$$[87r/(33-2F)]/(r \ln r). \quad (3.9)$$

However, traditionally this effect has been ignored by taking an average value of a_s at $q^2=m_c^2$. I consider that it is more appropriate to evaluate a_s at $q^2=(l/r)^2$. The average of $1/r$, $(\sqrt{r})^{1/2+3\alpha}$ for power-law confining potential $U(r)=kr^2/A$, where M is the reduced mass of the system. For the charmonium in the harmonic oscillator potential $\langle 1/r \rangle \approx 0.6$ GeV.

Of course we can use the Fourier transform of $a_s(q^2)/q^2$ as the one-gluon-exchange potential.⁴⁴⁺⁴⁵

Next let us discuss the hadronic decay width of T . According to QCD,⁵

$$\begin{aligned} \Gamma_h(Y) &\approx \Gamma(Y \rightarrow ggg) \\ &= (160/81)(\pi^2 - 9)(\alpha_s^3/M(Y)^2)|\phi(0)|^2 \end{aligned} \quad (3.10)$$

and⁶

$$\Gamma_{ee}(Y) = 16\pi\alpha^2 e_b^2 |\phi(0)|^2 / M(Y)^2. \quad (3.11)$$

Therefore,

$$\begin{aligned} \Gamma_h(Y)/\Gamma_{ee}(Y) &\approx (10/81\pi)(\pi^2 - 9)(\alpha_s^3/\alpha^2 e_b^2) \\ &= 19.5 \end{aligned} \quad (3.12)$$

for $\alpha_s=0.15$, which is derived from

$$\alpha_s(s) = \alpha_s(\mu^2) [1 + (23/12\pi)\alpha_s(\mu^2) \ln(s/\mu^2)]^{-1}, \quad (3.13)$$

and $\alpha_s=0.19$ for J/ψ . In (3.12) e_b stands for the charge of the b-quark.

The QCD prediction (3.12) seems somewhat smaller than the experimental result,³

$$\begin{aligned} r_h(r)/r_h(T) &= (>25 \text{ keV}; \text{ best value } 50 \text{ keV}) \\ &\times (1.3 \pm 0.2 \text{ keV}^{-1}). \end{aligned} \quad (3.14)$$

But, they are compatible if we make a correction for second order electromagnetic decays to the hadronic decay width of T .

There is an inequality on the mass of the b-quark,

$$m_c - m_s > 3.29 \text{ GeV} \quad (3.15)$$

derived by Grosse and Martin⁴⁶ for potentials which satisfy the conditions,

$$-\infty < \lim_{r \rightarrow \infty} [rV(r)] \leq 0 \quad (3.16)$$

and

$$(\Delta)W_0(r) > 0$$

and by making use of the experimental values of the masses of T , T' and J/ψ .

§4. Spectroscopy of Old Hadrons and QCD

Effective quark-quark interaction suggested by QCD, which has been applied to charmonium and T in the previous sections has been applied to the spectroscopy of old hadrons.

A long-range Lorentz-scalar confining force, together with a short-range Coulomb-like vector exchange has been applied to meson spectroscopy by Schnitzer.¹⁸ This interaction gives an excellent overall account of the spin structure of ordinary mesons, if $a_s(M)$ is sufficiently large as has been suggested by the violation of scaling in deep inelastic processes,

$$\alpha_s(M^2) = (12\pi/25)(\ln M^2/A^2)^{-1}$$

with $A=0.5$ GeV. Here, M is taken to be the mass of the bound state.

This model predicts the inverted *P multiplets for D and F charmed mesons and bottom mesons,^{1*147}

$$M(^3P_0) > M(^3P_1) > M(^3P_2).$$

The hyperfine interaction arising from a short-range Coulomb-like vector exchange with $a_s \sim l$ together with flavor independent long-range confining force has been applied to the spectrum and mixing angles of baryons by Isgur and Karl.^{48,49} They have found a good agreement in the $S=0$ and $S=-1$ sector (except for $4(1405) \text{ } ^1P=1/2$). They have discarded the spin-orbit interaction from the vector-exchange since they may be cancelled by the spin-orbit interaction from the long-range Lorentz-scalar confining force.

§5. Charmed Hadrons

The observation of the D and Z^* mesons were reported at the last conference. Last year candidates of the F and F^* mesons have been discovered at DESY with the following masses^{50,3}

$$M(F) = (2.03 \pm 0.06) \text{ GeV}$$

and (5.1)

$$M(F^*) - M(F) = (110 \pm 46) \text{ MeV.}$$

Some branching ratios of the D mesons have been measured. The observed branching ratio of the inclusive semileptonic decay is⁵¹

$$Br(D \rightarrow e\nu X) \approx 10\%. \quad (5.2)$$

If the nonleptonic decays of the D -mesons are not enhanced, we expect

$$Br(D \rightarrow e\nu X) \approx 20\%. \quad (5.3)$$

Thus the nonleptonic decays of the D -mesons are enhanced by a factor of about 8/3. Therefore, we do not have a serious problem such as the origin of the $|J|=1/2$ rule in the hyperon decays and $7\mathcal{L}$ -meson decays. In these decays $|A_1| = |j_2|$ part is enhanced by a factor of about 20.

Main part of the difference between (5.2) and (5.3) may be explained by QCD, in which nonleptonic decays are enhanced by a factor,⁵²

$$(2c_+^2 + c_-^2)/3 \approx 5/3, \quad (5.4)$$

and semileptonic decays are suppressed as much as 35%,⁵³ where

$$c_- = \{1 - [(33 - 2F)/12\pi] \alpha_s(m_c^2) \times \ln(m_W^2/m_c^2)\}^{1/2/(33-2F)}$$

and (5.5)

$$c_+ = (c_-)^{-1/3}.$$

In (5.4) we have used $c_- = 2.0$ and $c_+ = 0.7$ assuming $a_s(m_f) = 0.7$.

Because of the large masses, the charmed mesons decay into various channels and through the study of these decays we can test various models of weak nonleptonic decays. For example, by making use of the bounds⁵⁴

$$0 < r(D^+)/r(D^0) < 3, \quad (5.6)$$

which are imposed by the $|J|=1$ rule, and the measured branching ratios of $D^+ \rightarrow K^- 7r^+ 7r^+$ and $J^0 \rightarrow K^- 7r^+ 7r^0$,⁵⁵ it has been shown that the matrix elements of some of $D \rightarrow K n 7t$ decays cannot be uniform over the Dalitz plot^{56,57,59}. It has been suggested that $D^+ K^- 7t x^0$ decay is dominated by $K \sim p^+$ states.⁵⁷

§6. ν

All observed properties of r are consistent with those of a new sequential heavy lepton.^{61,60} (See, Table II.)

Table II. r decays

Decay mode	Experiment	Theory ⁶¹
$e\nu\bar{\nu}$	$16.9 \pm 1.9\%$	$\sim 18\%$
$\mu\nu\bar{\nu}$	$18.3 \pm 1.9\%$	$\sim 18\%$
$\pi\nu$	$7.7 \pm 1.3\%$	$\sim 10\%$
$\rho\nu$	$24 \pm 9\%$	$\sim 22\%$

If T is a bound state of a b -quark and its antiparticle, and if the b -quark and the t -quark belong to a doublet of the weak $SU(2)$ group, we find a beautiful correspondence between

$(w, d), (c, s)$ and (t, b) ,

and

$(e, \nu), (p, \quad)$ and (r, ν_r) .

§7. Baryonium

In the nonrelativistic quark model a baryon is a bound state of three quarks, and a meson is a bound state of a quark and an antiquark.

However, there are some indications that there might be other types of mesons.

For example, several narrow peaks have been observed in pp system³

Name	Mass (MeV)	Width (MeV)	Remarks
S	1936 ± 1	$< 4 \sim 8$	$\bar{p}p$ formation experiment, ⁶²
—	2020 ± 3	$\lesssim 10 - 20$	baryon exchange reaction, ⁶³
—	2204 ± 5	$\lesssim 10 - 20$	

Here S(1936) is a narrow resonance with a large elasticity. There are additional indications of narrow resonances with $i^P = 0$.⁶⁴

It is difficult to regard the narrow resonances observed in PP system, such as S(1936), as mesons which consist of a quark and an antiquark. These resonances have narrow widths of about 10 MeV in spite of their high masses. They are characterized by their reluctance for decaying into meson states, as inferred either from the measured branching ratios, or from their small total widths. That is, their couplings with mesons are weak. Therefore, they are popularly called "baryonium".^{56,5}

Necessity of such resonances was advocated by Rosner when duality was applied to baryon-antibaryon reactions^{66,67}. In order to draw duality diagrams for $BB \rightarrow BB$ we have to introduce resonances which consist of two quarks and two antiquarks ($iqqq$) (Fig. 7.1). If the $qqqq$ resonances couple strongly with

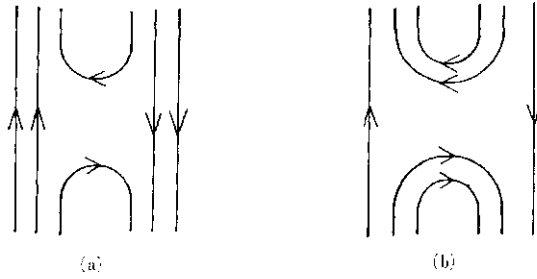


Fig. 7. 1. Duality diagrams for $B\bar{B} \rightarrow B\bar{B}$.

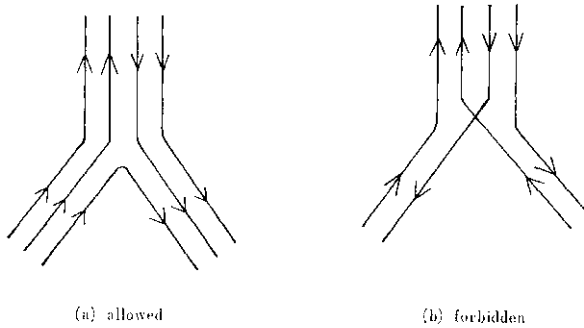


Fig. 7. 2. Freund-Waltz-Rosner rules, (a) allowed; (b) forbidden.

two-meson states, we cannot expect that the vector and tensor trajectories are exchange degenerate. Therefore, the $qqqq$ resonances are not allowed to couple strongly with meson states in dual models.

Thus, the following selection rules for the vertices were proposed by Freund, Waltz and Rosner⁶⁸;

(1) Every quark-line connects two different hadrons. (OZI rule)

(2) Every pair of the hadrons must be connected by at least one quark-line.

According to these rules, the decays of the $qqqq$ resonance into BB states are allowed but the decays into meson states are forbidden. (See Fig. 7.2.)

If the baryonium is a $qqqq$ resonance, we have to explain how two quarks and two antiquarks are bound together and why it cannot decay into mesons strongly. In order to answer these questions we have to know how a quark-antiquark pair and three quarks are confined to the interior of mesons and baryons, respectively.

There are several models of hadrons. As examples let us consider the junction model^{69,71} and the bag model.⁷²⁻⁷⁴

7.7 Exotic mesons in the junction model

In the junction model mesons are bound

states of a colored quark and a colored anti-quark bound by a colored oriented string (Fig. 7.3 (a)). Baryons consist of three colored quarks, each of which is tied at the end of three colored oriented strings, and the three strings are joined at a point called the string "junction"^{69,70} (Fig. 7.3(b)).^{75,76}

The meson and baryon in this model shown in Fig. 7.3 correspond to the following color gauge invariant operators,⁷¹

$$\bar{\psi}^i(x)[G(P(x, y))]_i^j \psi_j(y) \tag{7.1}$$

and

$$e^{*} \gg [G(P(x, y)W(y)MG(P(x, z))^{(z)}, X [\% w M 4 \tag{7.2}$$

respectively, where

$$[G(P(x, y))]_i^j = \left[T \exp \int_{P(x, y)} A_{\mu}(x) dx^{\mu} \right]_i^j \tag{7.3}$$

and ij and k are color SU(3) indices.

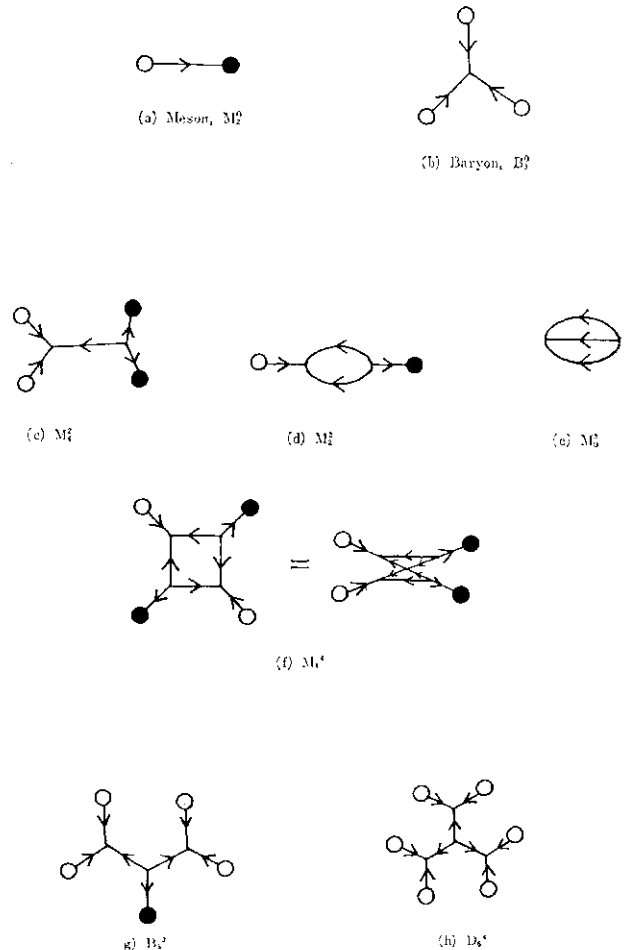


Fig. 7. 3. Various types of hadrons in the junction model.

(a) Meson, M_2^0 ; (b) Baryon, B_3^0 ; (c) M_4^2 ; (d) M_2^2 ; (e) M_0^2 ; (f) M_4^4 ; (g) 5_5^3 ; (h) D_5^* .

In the junction model baryons consist of three colored quarks (tied at the ends of three strings) and a junction. Hence, we draw junction lines (broken lines) as well as quark lines (solid lines) in duality diagrams.

Various hadrons of new types can be constructed of quarks and junctions. In Fig. 7.3 some of possible types of hadrons in this model, M_l , M_l , M_l , M_i , B_l and D_l are also shown. Here, the superscripts are the numbers of the junctions, N_j , and the subscripts are the numbers of the quarks and antiquarks, N_q .

Since hadrons are regarded to consist of quarks and junctions, Freund-Waltz-Rosner rules for vertices are enlarged as follows⁷⁷:

- (1) Every quark-line and every junction-line connect two different hadrons.
- (2) Every pair of hadrons must be connected by at least one quark-line or one junction-line.

These rules are called covalence rules by Imachi and Otsuki.⁷⁷

Then, the following decays into meson states are forbidden by the rules (1) and/or (2), (Fig. 7.4)

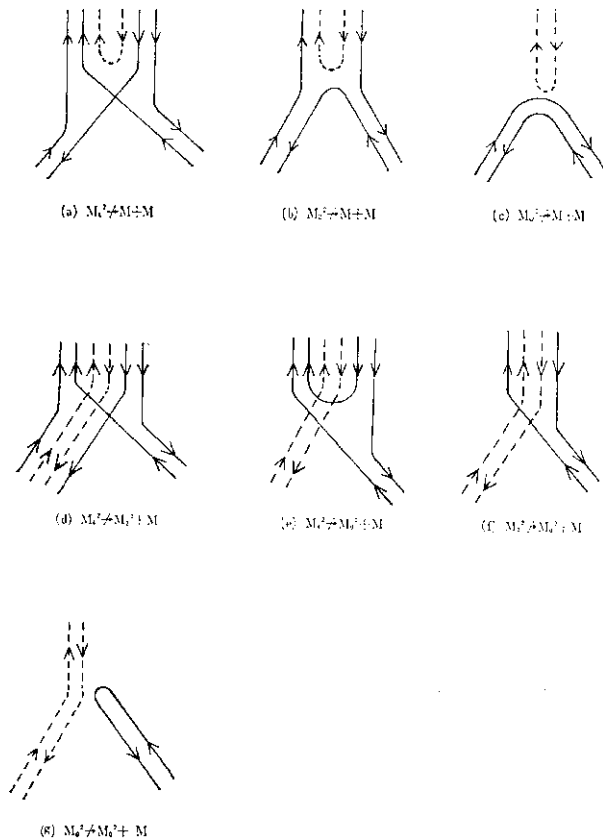


Fig. 7.4. Forbidden decays of baryonium.
 (a) $M_4^2 \rightarrow M+M$; (b) $M_2^2 \rightarrow M+M$; (c) $M_0^2 \rightarrow M+M$;
 (d) $M_4^2 \rightarrow M_2^2+M$; (e) $M_4^2 \rightarrow M_0^2+M$; (f) $M_2^2 \rightarrow M_0^2+M$;
 (g) $M_0^2 \rightarrow M_0^2+M$.

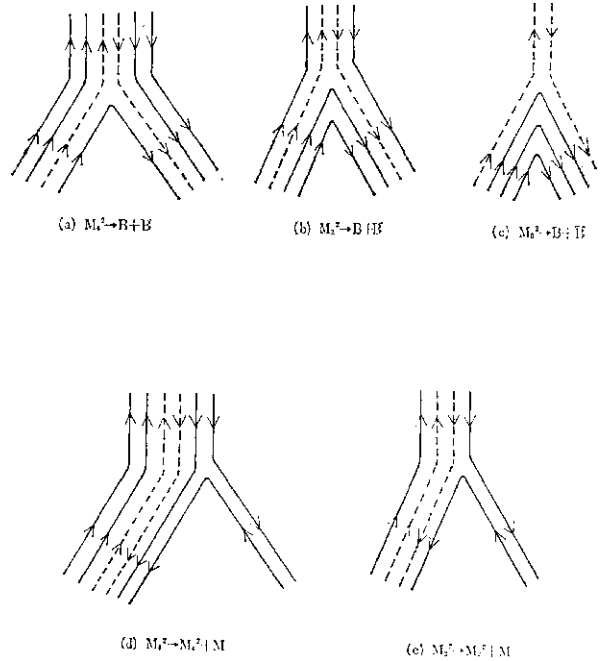


Fig. 7.5. Allowed decays of baryonium.
 (a) $M_4^2 \rightarrow B+B$; (b) $M_2^2 \rightarrow B+B$; (c) $M_0^2 \rightarrow B+B$;
 (d) $M_4^2 \rightarrow M_4^2+M$; (e) $M_2^2 \rightarrow M_2^2+M$.

$$\begin{aligned}
 &M_4^2 \leftrightarrow MM, M_2^2 \leftrightarrow MM, M_0^2 \leftrightarrow MM, \\
 &M_4^2 \leftrightarrow M_2^2 M, M_4^2 \leftrightarrow M_0^2 M, M_2^2 \leftrightarrow M_0^2 M, \\
 &M_0^2 \leftrightarrow M_0^2 M,
 \end{aligned} \tag{7.4}$$

but the following decays into BB states are allowed, (Fig. 7.5)

$$M_4^2 \rightarrow B\bar{B}, M_2^2 \rightarrow B\bar{B}, M_0^2 \rightarrow B\bar{B}. \tag{7.5a}$$

Therefore, we may call M_l , M_l and M_l baryonium. The mesonic decays of baryonium, M_l and M_l , into the baryonium of the same type \bar{B} are also allowed, (Fig. 7.5).

$$M_4^2 \rightarrow M_4^2 M, M_2^2 \rightarrow M_2^2 M. \tag{7.5b}$$

The allowed decays of baryonium occur through string breaking and fusion of "active" quarks created by the breaking.

There are several attempts to justify the covalence rules from the exchange degeneracies of baryons.^{75, 78, 79}

In Fig. 7.6 we show some of the duality diagrams in this model. From the duality diagrams, we find that the Regge trajectories a'_q of the baryonium M'_q , $a(s)$, $a(s)$ and $a(s)$ are dual with ordinary meson trajectory $a_n(s)(=a(s))$, two-meson (MM) cut and three-meson (MMM) cut, respectively. The effective slopes of MM -cut and MMM -cut are $(1/2)a'$ and $(1/3)a'$, respectively. Therefore, we obtain

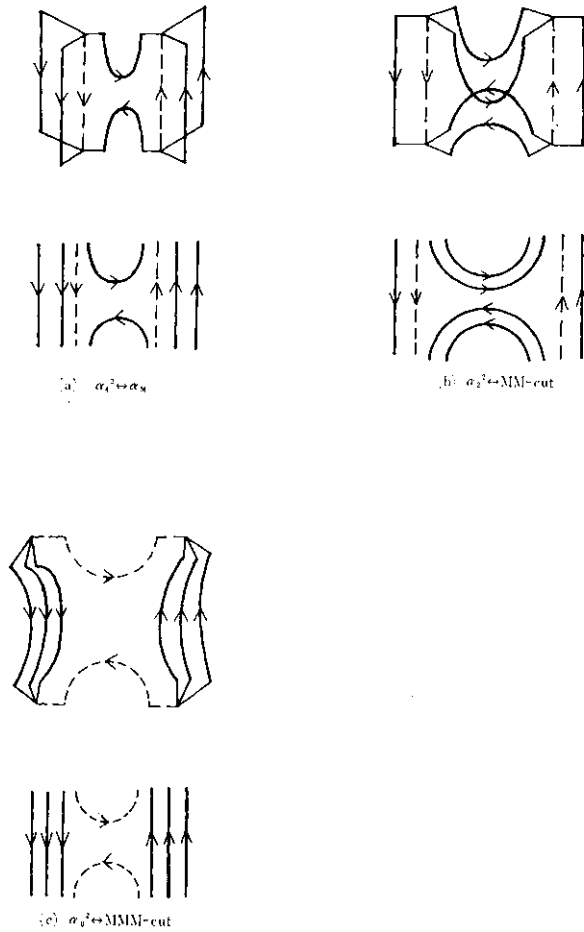


Fig. 7. 6. Duality diagrams in the junction model. (a) $\alpha_4^2 \leftrightarrow \alpha_M$; (b) $\alpha_2^2 \leftrightarrow MM$ -cut; (c) $\alpha_0^2 \leftrightarrow MMM$ -cut.

$$\alpha_4^{2'} \approx \alpha', \alpha_2^{2'} \approx (1/2)\alpha', \text{ and } \alpha_0^{2'} \approx (1/3)\alpha' \tag{7.6}$$

from semilocal duality.⁷¹⁷⁹

According to the dual unitarization scheme,⁸⁰ we find the following rule for the zero-intercepts,⁸¹

$$\alpha_{N_q}^{N_f}(0) \approx 1 - (1/4)N_q - (1/4)N_f - (1/4)N_s, \tag{7.7}$$

where N_i is the total number of i -quark and \bar{i} -quark.

Therefore, assuming linear trajectories for the baryonium, we obtain

$$\begin{aligned} \alpha_4^2(s) &\approx -0.5 + \alpha's, \\ \alpha_2^2(s) &\approx (1/2)\alpha's, \\ \alpha_0^2(s) &\approx 0.5 + (1/3)\alpha's. \end{aligned} \tag{7.8}$$

(See, Fig. 7.7.)

I will not try to assign observed narrow resonances to some of M^2 states in this talk.^{79, 82} Of course, it is possible to assign some of them to M^{**} .⁸¹

7.2 $qqqq$ states in the bag model

In the bag model colored quarks and anti-quarks are confined to the interior of a finite domain called a bag. In this model long-range confining forces are replaced by the bag pressure, B . There are the following contributions to a hadron mass in the model⁷²⁻⁷⁴; 1) the quark mass and kinetic energy; 2) the energy stored in the confining forces (bag energy); 3) the finite energy associated with zero-point energies of the fields confined to the bag; (We have to include this energy since it is dependent on the radius of the bag, R .) and 4) the spin-spin interaction arising from one-gluon exchange;

$$M = \sum_i \frac{\alpha_i(R)}{R} + \frac{4\pi}{3} R^3 B - \frac{Z_0}{R} + \sum_{ij} V_{ij}(R). \tag{7.9}$$

The bag model has been successful in describing the spectrum of light hadrons ($1/2^+$ and $3/2^+$ baryons, 0^- and 1^- mesons),⁷⁴ and can be applied to $qqqq$ states without introducing new parameters.⁸⁵ In the bag model $L=C$ $qqqq$ states are constructed by populating quark modes in a bag. Jaffe and Johnson⁸⁵ found the lowest mass $qqqq$ states to be an $SU(3)$ nonet of scalar mesons with masses ranging from 645 to 1120 MeV,

E_K^+ ; $ud\bar{s}\bar{d}$, E_K^0 ; $ud\bar{s}\bar{u}$,	~ 880 MeV,
E_K^0 ; $us\bar{u}\bar{d}$, E_K^- ; $ds\bar{u}\bar{d}$,	~ 880 MeV,
E^+ ; $us\bar{d}\bar{s}$, E^0 ; $(us\bar{u}\bar{s} - ds\bar{d}\bar{s})/\sqrt{2}$,	
E^- ; $ds\bar{u}\bar{s}$,	~ 1120 MeV,
E_2^0 ; $(us\bar{u}\bar{s} + ds\bar{d}\bar{s})/\sqrt{2}$,	~ 1120 MeV,
E_1^0 ; $ud\bar{u}\bar{d}$,	~ 645 MeV,

by making use of the parameters used in describing the spectrum of the light hadrons.

They have suggested that the scalar nonet [$e(700)?$, $S^*(993)$, $3(980)$, $4800-1100$] ⁸⁶ should be identified with the above scalar $qqqq$ nonet than with the 3P_0 nonet of the conventional nonrelativistic quark model.

In the bag model $L=0$ $qqqq$ states are expected to be broad. A broad $qqqq$ state can simply fall apart into two qq mesons.

Higher orbital angular momentum states are obtained by rotating the bag with a diquark in one side and an antiquark in another side of an elongate bag. There are two quark configurations.⁸⁷ In one con-

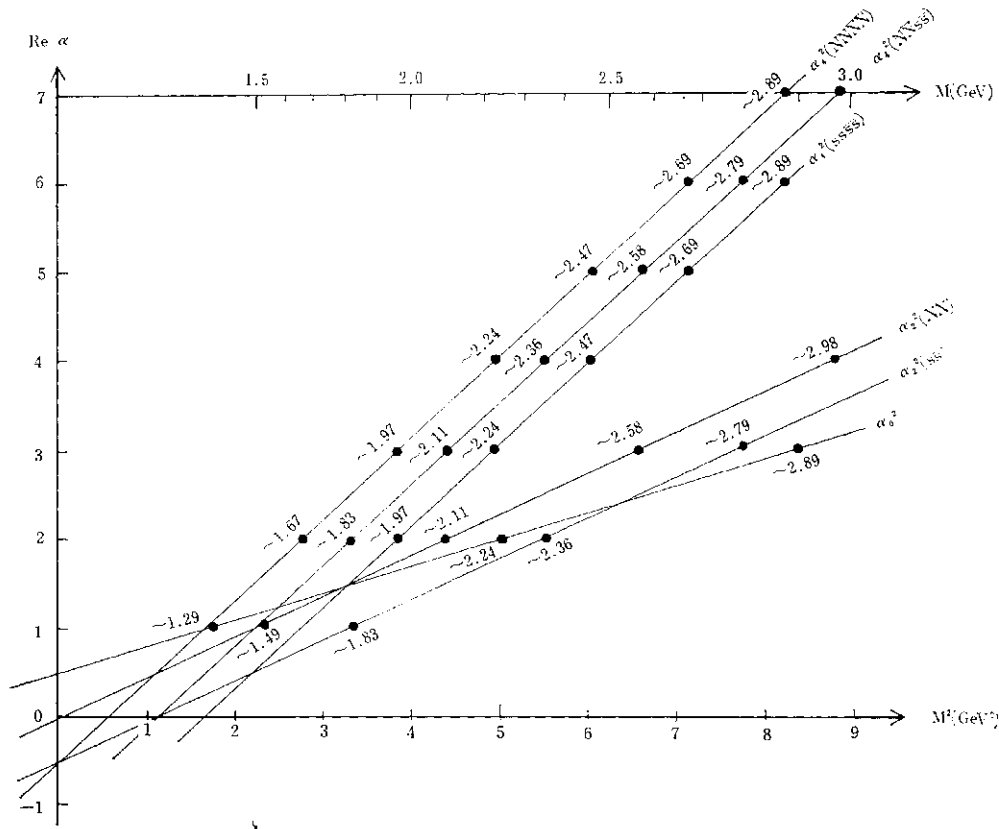


Fig. 7.7. Regge trajectories of baryonium (for $\alpha' = 0.9 \text{ GeV}^{-2}$). Here, leading trajectories $\alpha_4^2(NNNN)$, $\alpha_4^2(NNs)$, $\alpha_4^2(sss)$, $\alpha_2^2(NN)$, $\alpha_2^2(ss)$ and α_0^2 are shown, where N stands for u and/or d .

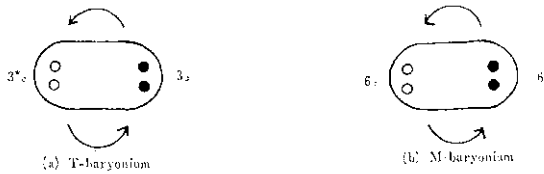


Fig. 7.8. $qq\bar{q}\bar{q}$ states with high spin in the bag model. (a) T-baryonium; (b) M-baryonium.

figuration both the diquark and the antiquark are color-triplets (T-baryonium) and in another configuration both are color-sextets (M-baryonium),⁸⁸ *i. e.*,

$$(qq)_{3^*} - (\bar{q}\bar{q})_3, \quad (\text{T-baryonium})$$

and

$$(qq)_6 - (\bar{q}\bar{q})_{6^*}, \quad (\text{M-baryonium}).$$

(Fig. 7.8)

Two types of the $qq\bar{q}\bar{q}$ states lie on Regge trajectories with different slopes. Let us discuss the slopes of the Regge trajectories. Asymptotically for large mass, we expect the trajectories to be linear in M^2 . In the bag model the slope is proportional to $(\delta^2) \sim 1/2$, where Q^2 is the quadratic Casimir for the color SU(3) representation inside the bag,⁸⁹

$$Q^2 = 16/3 \quad \text{for } 3, \\ = 40/3 \quad \text{for } 6. \quad (7.10)$$

Therefore, the T-baryonium slope α'_T is the same as that for ordinary qq mesons,

$$\alpha'_T = \alpha' \approx 1 \text{ GeV}^{-2} \quad (7.11a)$$

and the M-baryonium slope is given by

$$\alpha'_M = \sqrt{2/5} \alpha'_T \approx 0.63 \text{ GeV}^{-2}. \quad (7.11b)$$

The T-baryonium and M-baryonium have very different physical properties.⁸⁸ Although both are expected to have inhibited decays into pions because of the angular momentum barrier, they have different couplings to BB . The diquark in a T-baryonium state, being in a 3^* representation, can combine with another quark in a 3 representation to form a color singlet baryon. (Fig. 7.9(a).) Therefore, the T-baryonium couples strongly with BB channel and is expected to have a decay width of ~ 100 MeV. Whereas M-baryonium⁹⁰ cannot decay in this manner, since the diquark in a 6-representation when combined with another quark in 3 does not give a color singlet ($6 \times 3 = 10 + 8$). They are, therefore, weakly coupled both to meson and BB channels (Fig. 7.9(b)-(e)), and prefer to decay by cascade into a

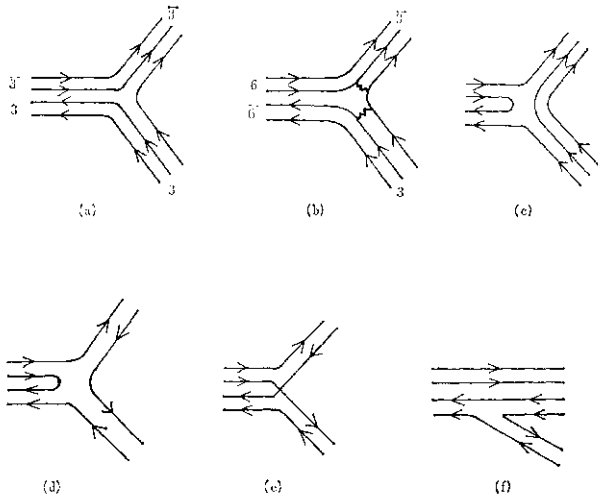


Fig. 7.9. Decays of T-baryonium and M-baryonium

resonance of the same type⁸⁸ (Fig. 7.9(f)).

Observed narrow resonances have been assigned to baryonium states by Chan and Hogaasen.^{88,84}

Finally let us discuss the stability of the baryonium.⁹¹

The mass of T- and M-baryonium have been estimated by Barbour and Ponting⁹² in variational method by making use of a model Hamiltonian. According to their results, in the T-baryonium case the two $q\bar{q}$ -meson states, through which baryonium may decay into meson final states, are generally found to be more massive than the baryonium state itself, but in the M-baryonium case they are lighter than the baryonium state.

However, asymptotically for large mass, the M-baryonium with spin J is lighter than the two g Λ -mesons with spin $J/2$ since⁹³ $2a'_m > a'$; Since the mass (M) of the M-baryonium with spin J is $\ll j\bar{j}\bar{a} = (j5j2J/ay^2)$ ($\sim a'_m M$) and since the mass (m) of the qq -meson with spin $J/2$ is $\ll j/2a'$ ($J/2 \sim a'm^2$), $2m \ll \sqrt{2J/a'} \sim (5/2)^{1/4} \sqrt{VJJa'} \sim M$. Notice, however, this argument is applicable only when $|\sigma(\mathbf{0})| < 1$.

§8. Dibaryons

Once pp total cross sections were considered

to be roughly energy independent.⁹⁴ If they are independent of energy, there should be no hadrons with baryon number two in dual models.

Recently a remarkable energy dependence has been discovered in measurements of pp total cross sections with a polarized beam and target,⁹⁵ and several evidences on the existence of the hadrons with baryon number two listed in Table III have been reported.⁹⁵⁻¹⁰¹

$5^2(2.14)$ and $B(2.22)$ are characterized by their small elasticity.

The deuteron is not listed in the table since it is not a hadron, but a nucleus, *i. e.*, a bound state of a proton and a neutron bound by nuclear force. To regard the deuteron as a six-quark state is not adequate.¹⁰³ In the terminology of the quark model it is a molecular state of two clusters of three-quarks bound by colorless interaction.

Then, are $5^2(2.14)$ and $5^2(2.22)$ the subject of this conference, *i. e.*, are they nuclei or hadrons? I would like to regard them as hadrons because of their small elasticity and their small sizes.

The bag model has been applied to dibaryon resonances.^{104,105} In the bag model $L=0$ six-quark states are constructed by populating quark levels in a bag. The predicted energy levels are

$$I=1; \quad {}^1S_0 (M=2.24 \text{ GeV}),$$

$${}^1D_2 (M=2.36 \text{ GeV})$$

$$I=0; \quad {}^3S_1 (M=2.16 \text{ GeV}),$$

$${}^3D_3 (M=2.36 \text{ GeV}).$$

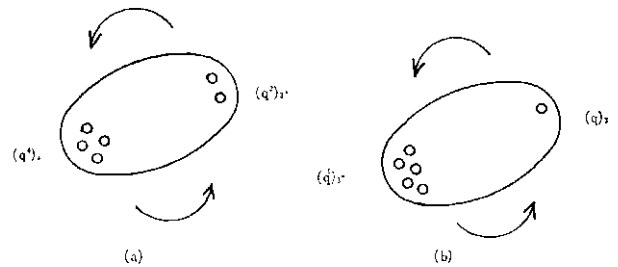


Fig. 8.1. Dibaryon resonances in the bag model (a^*0)..

Table III. Dibaryon resonances.

Name ¹⁰²	Mass (GeV)	Width (MeV)	I	NN-state	Elasticity	Remarks
$B^2(2.14)$	2.14-2.17	50-100	1	1D_2	0.1	$\Delta\sigma_L, \Delta\sigma_T$ etc. ⁹⁵⁻⁹⁸
$B^2(2.22)$	2.20-2.26	100-150	1	3F_3	0.2	$\Delta\sigma_L$ etc. ^{95,96,99}
$B^2(2.43)$	2.43-2.50	150	1	1S_0 or 1G_4		$\Delta\sigma_L, \Delta\sigma_T, C_{LL}$ etc. ⁹⁶
$B^2(2.38)$	2.38	?	0?	?		$\gamma d \rightarrow np$ _{100,101}

$L=l$ negative parity resonances are obtained by rotating the bags with the following clusters of quarks in two ends,

$$(q^4)_3 - (q^2)_3^*, (q^5)_3^* - (q)_3 \text{ etc.}$$

(See, Fig. 8.1.) Mulders, Aerts and de Swart have estimated the masses of dibaryon states in the bag model.¹⁰⁵ Some states occur with quantum numbers foreign to NN states, which they refer to as extraneous states.

§9. Concluding Remarks

Any talk on particle spectroscopy is incomplete unless something is mentioned about the quarks.

An expert on English literature told me that there were four seagulls in a dence fog when Tristan and Isolde heard three quarks.¹⁰⁶

Now we have already found five seagulls and it seems that there is at least one more seagull in a fog. Let me speculate that this sixth seagull will be discovered before next Conference.

Acknowledgments

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$$M(^3S_1) - M(^1S_0) = \frac{32\pi}{9m_c^2} \alpha_s |\psi(0)|^2 + \frac{4}{3} \frac{fa(1+\kappa)^2}{m_c^2} \langle r^{-1} \rangle_{S\text{-wave}}$$
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87. These two types of states do not mix when the orbital angular momentum L (of the diquark about the antiquark) is large because of the following reason. From one-gluon-exchange we obtain a spin-spin interaction between the two quarks of the following form,

$$a = 1$$

where C is proportional to the quark-gluon coupling a , and depends on the overlap of the quark spacial wave functions with the potential. Two quarks may couple to a 3^* or 6 of color SU(3) and a spin singlet or triplet. The diquark system can thus be in the following representations with the eigenvalue AE of the spin-spin interaction

(color, spin)	Flavor	ΔE
$(3^*, 1)$	3^*	$-8C$
$(6, 3)$	3^*	$-(4/3)C$
$(3^*, 3)$	6	$(8/3)C$
$(6, 1)$	6	$4C$

Since the color magnetic forces between the quarks and the antiquarks are short-ranged, their effect should decrease rapidly with L . At high L , therefore, there are no interaction which mixes the color-triplet diquark and the colorsextet diquark. For detail see ref. 88.

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90. The M-baryonium may correspond to the M_i^+ meson in the junction model shown in Fig. 7.3 (f). The decays of M_i^+ into $M_i^+ + M$, $B+B_s$, $B+B+B+B$ etc. are allowed, but the decay of M_i^+ into $B+B$ is forbidden. There is also a possibility that there may be a new type of strings, at the ends of which diquarks and antidiquarks in color sextets are tied. The allowed decay of the new $qqqq$ state tied with the new string M_i^+ is $M_i^+ \rightarrow M_i^+ + M$.
91. Quantitative calculation of $qqqq$ states has been carried out in (3+1) dimensional lattice gauge theory by Sakai and Hikosaka, and they have obtained the result, $M(qqqq)/M(N) = 2.8$; S. Sakai and K. Hikosaka: Paper No. 250 submitted to this Conference. In this model the results, $M(\hat{u}O \ll M(\hat{O})) \ll 0.82Af(N)$, have already been obtained by Banks, *et al.*; T. Banks, *et al.*: *Phys. Rev.* D15 (1977) 1111.
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P6: eN , fiN , rN Reactions

Chairman: W. PAUL

Speaker: E. GABATHULER

Scientific Secretaries: K. KONDO
T. SATO